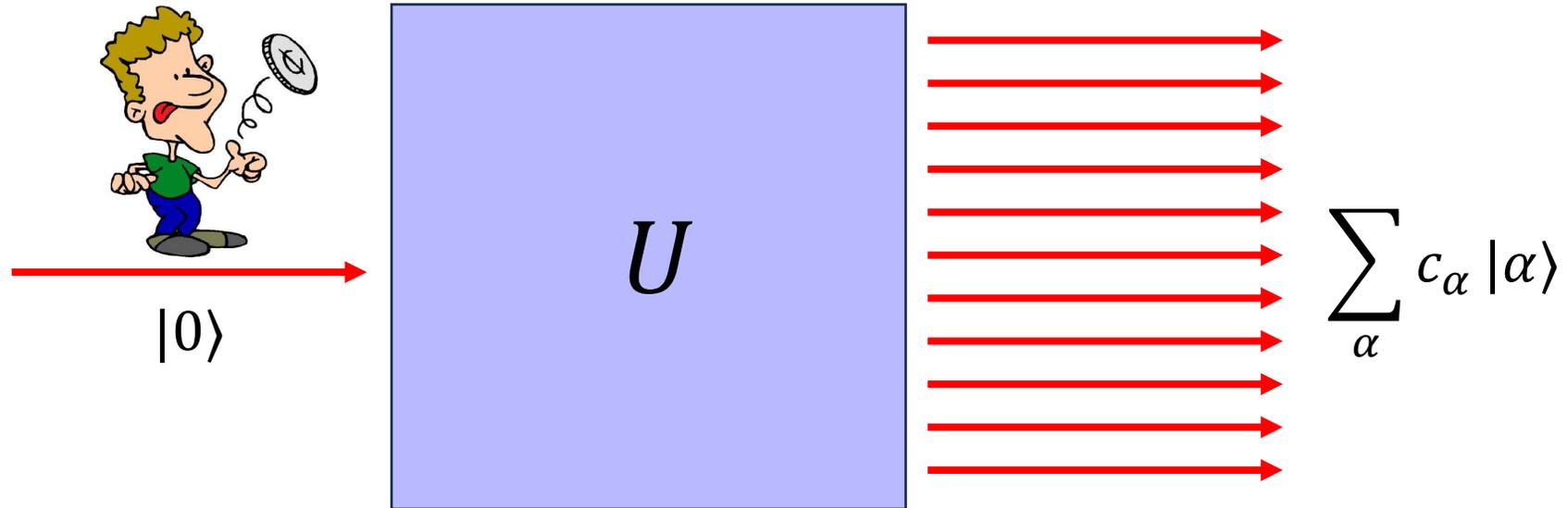


# Large-scale quantum walks via complex polarization transformations



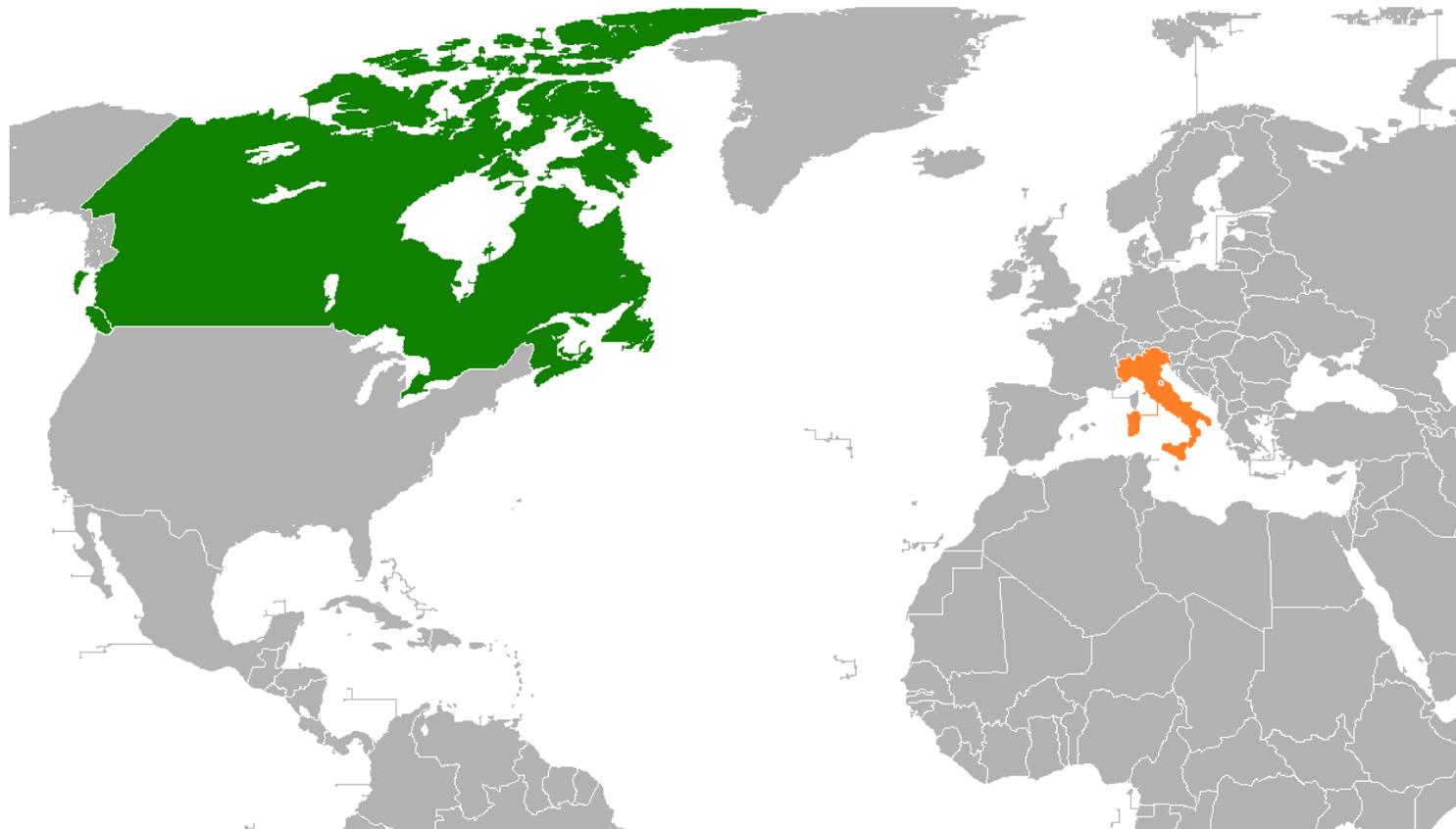
UNIVERSITÀ DEGLI STUDI  
DI NAPOLI FEDERICO II

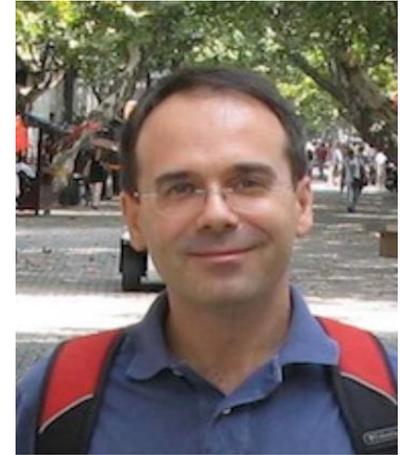
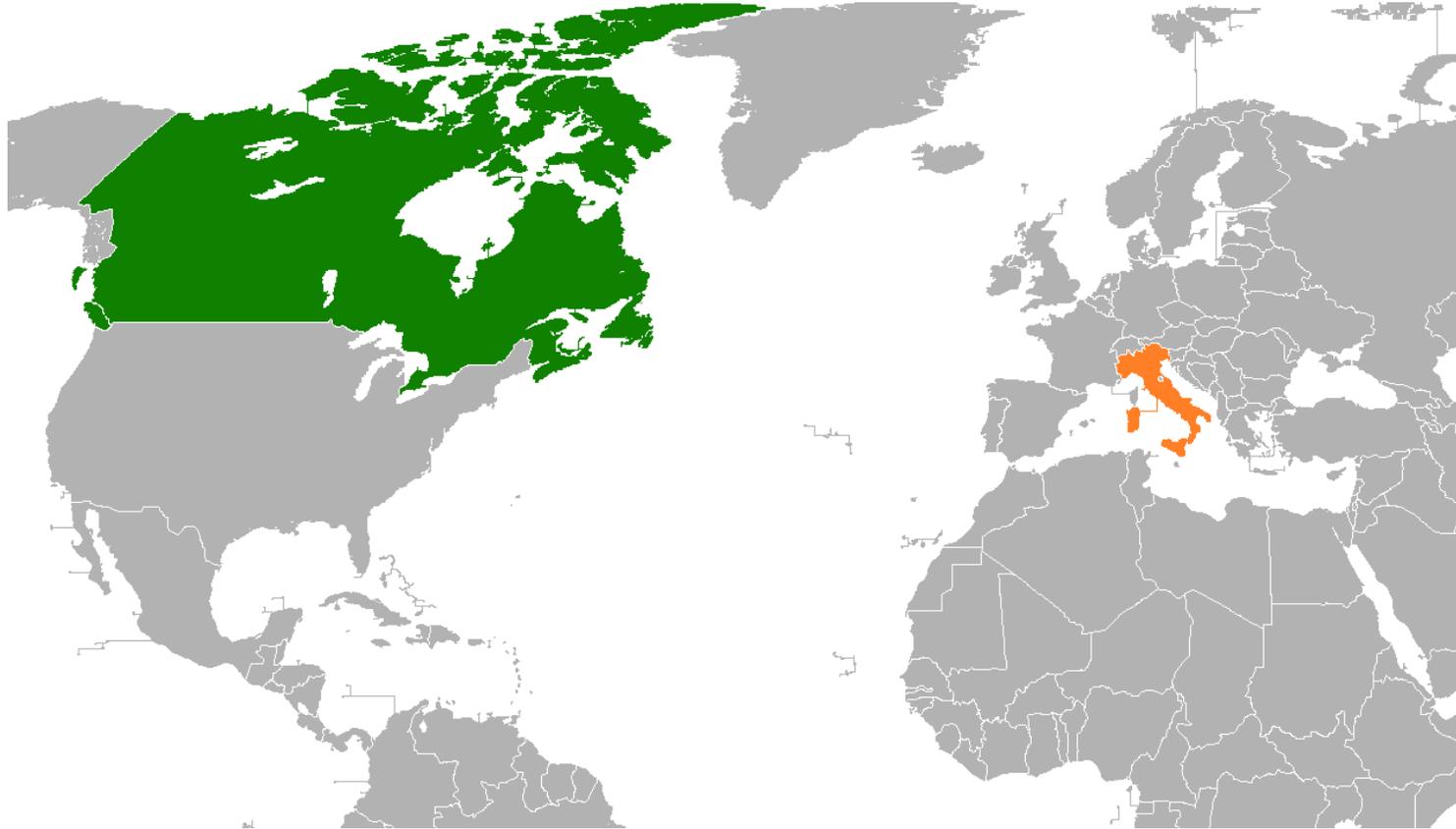


uOttawa

**Francesco Di Colandrea**

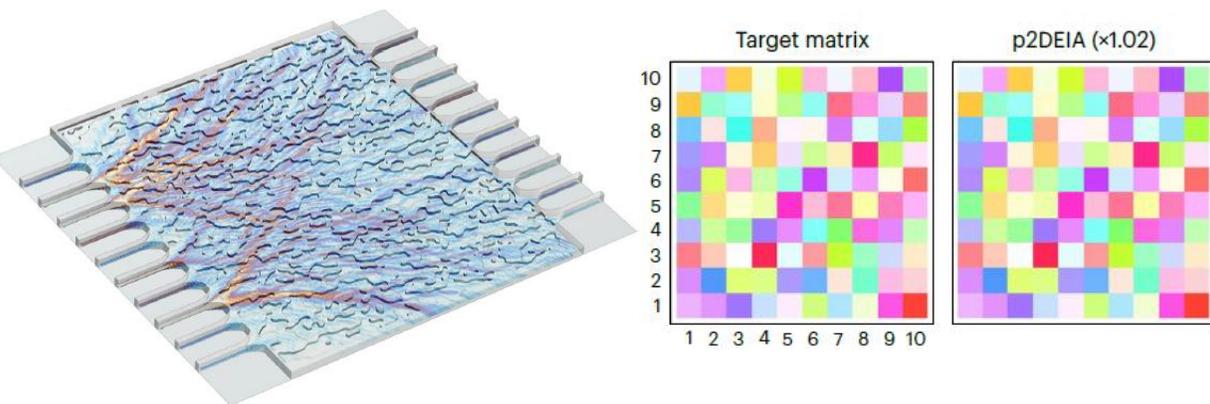
11<sup>th</sup> International conference on  
Quantum Simulation and Quantum Walks





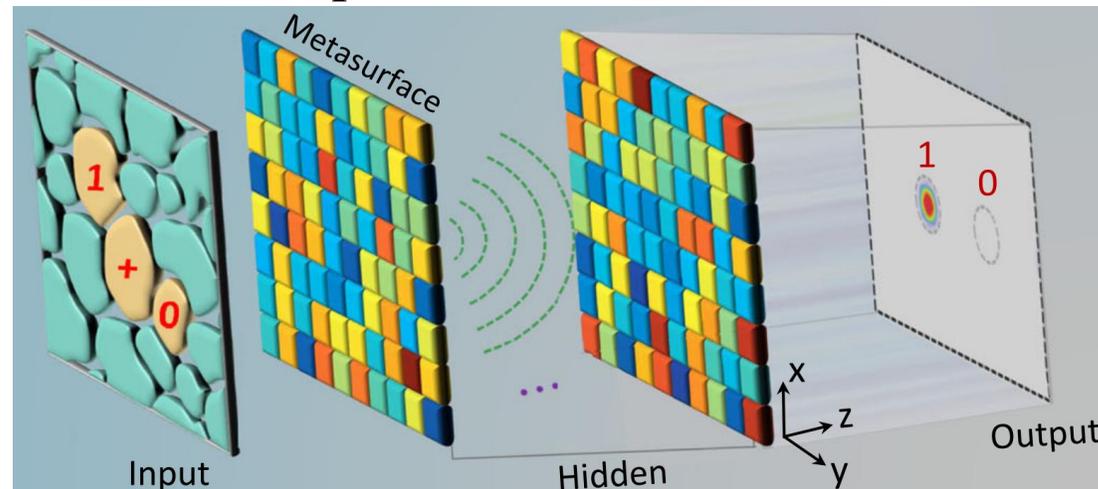
# *Photonic circuits*

## Analogue computation



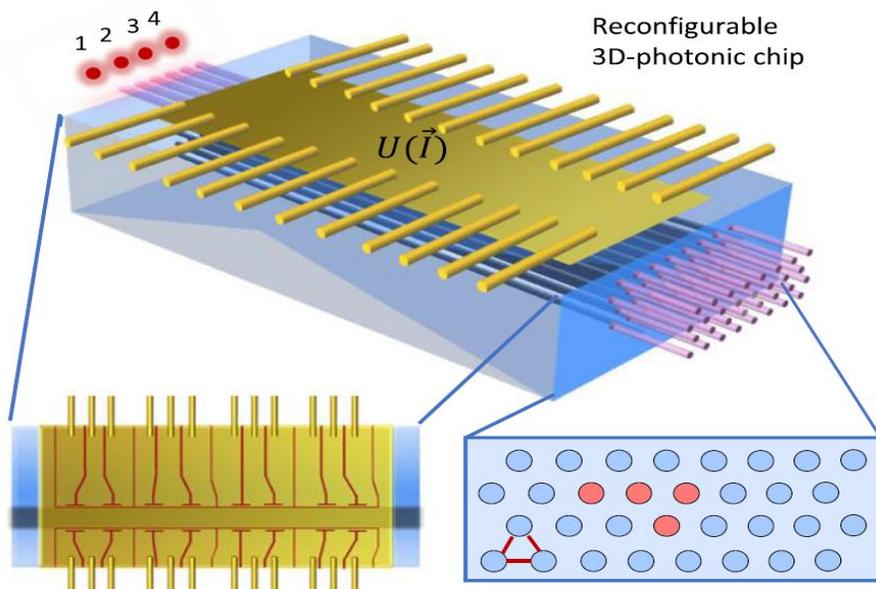
V. Nikkhah et al., Nat. Photonics 18, 501 (2024)

## Optical neural networks



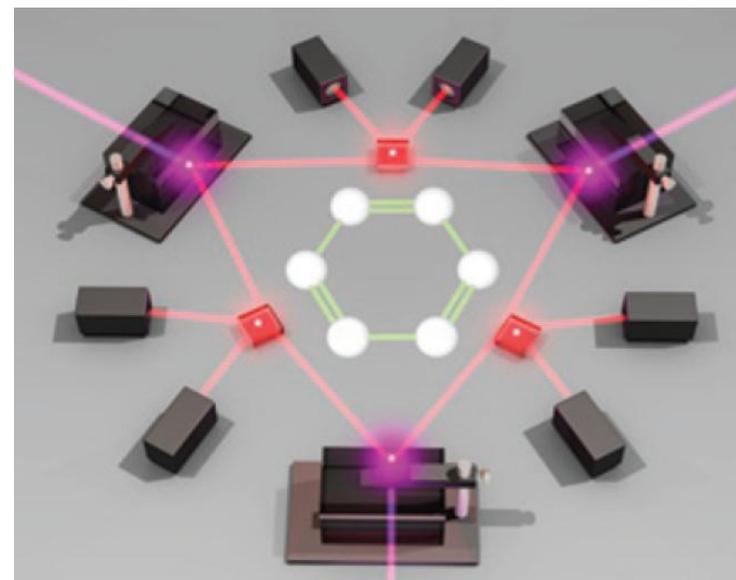
C. Qian et al., Light Sci. Appl. 9, 59 (2020)

## Unitary operations



F. Hoch et al., npj Quantum Inf. 8, 55 (2022)

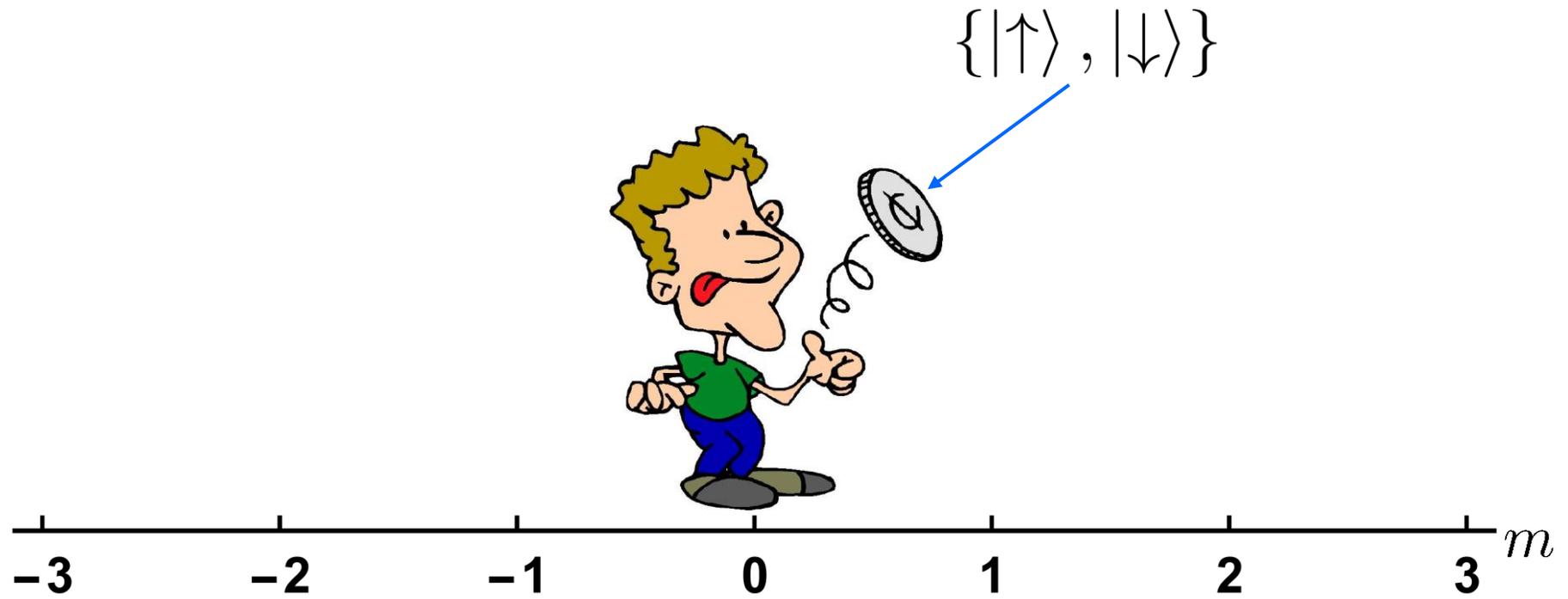
## Quantum simulations



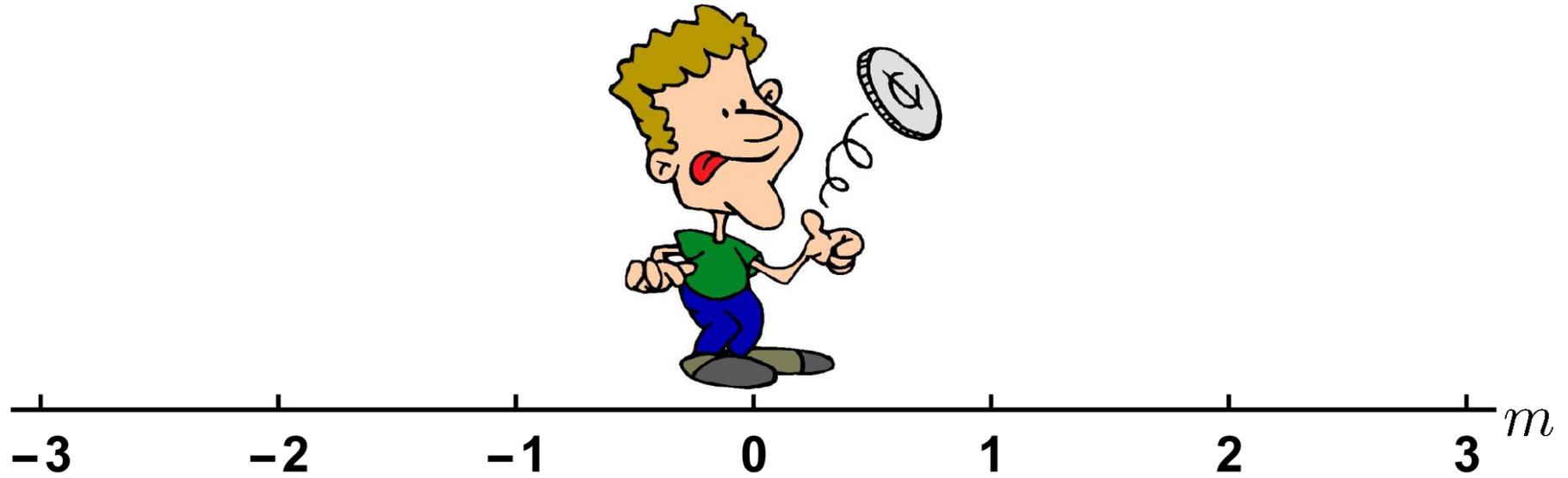
A. Aspuru-Guzik and P. Walther, Nat. Phys. 8, 285 (2022)

*Quantum walks*

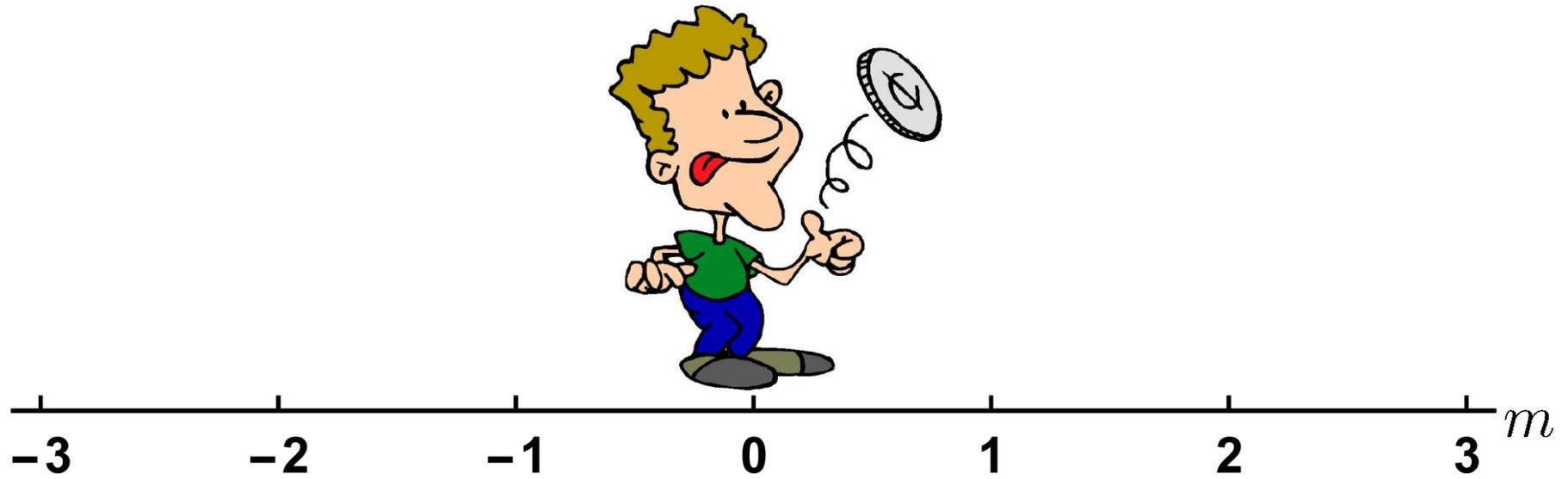
# The quantum walk



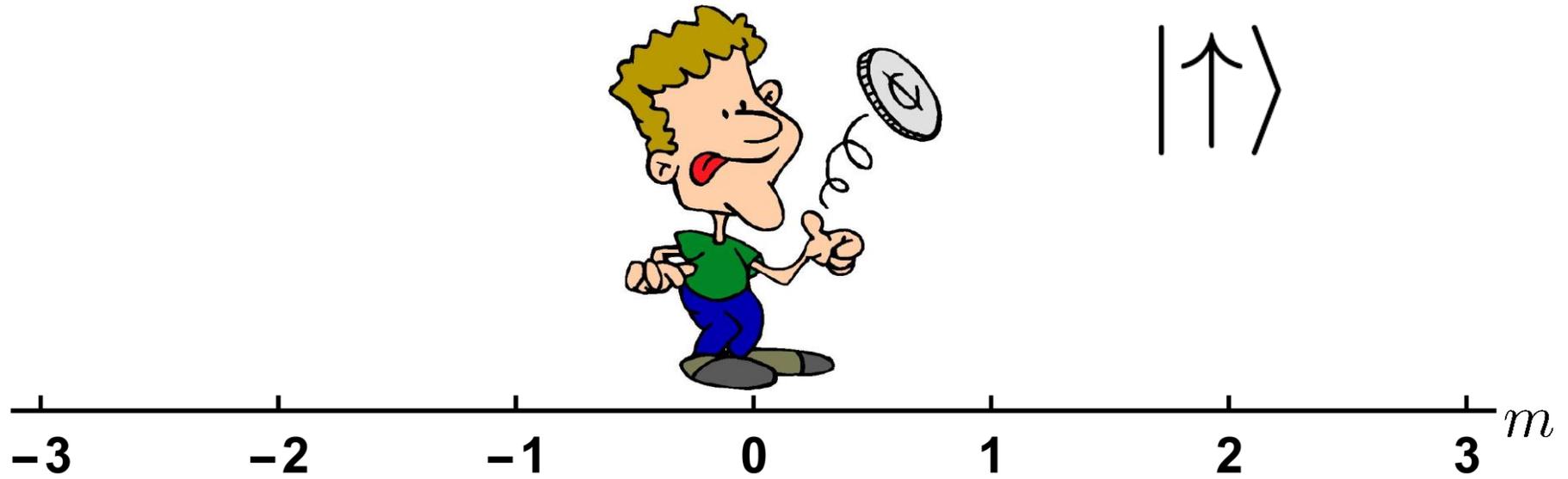
- A few rules:
- 1) Toss the coin
  - 2) Move according to the coin state
  - 3) Repeat



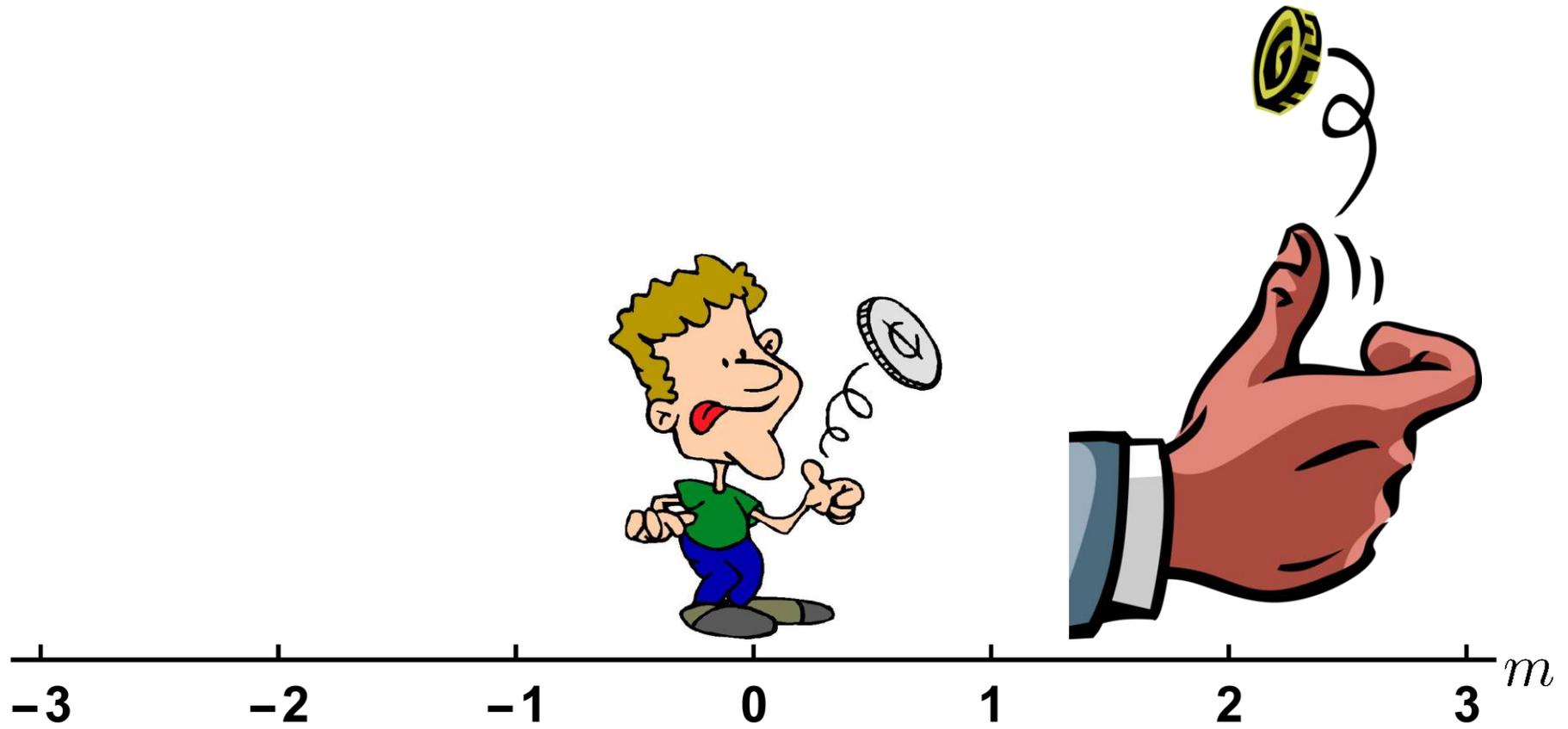
Let's (quantum) walk!



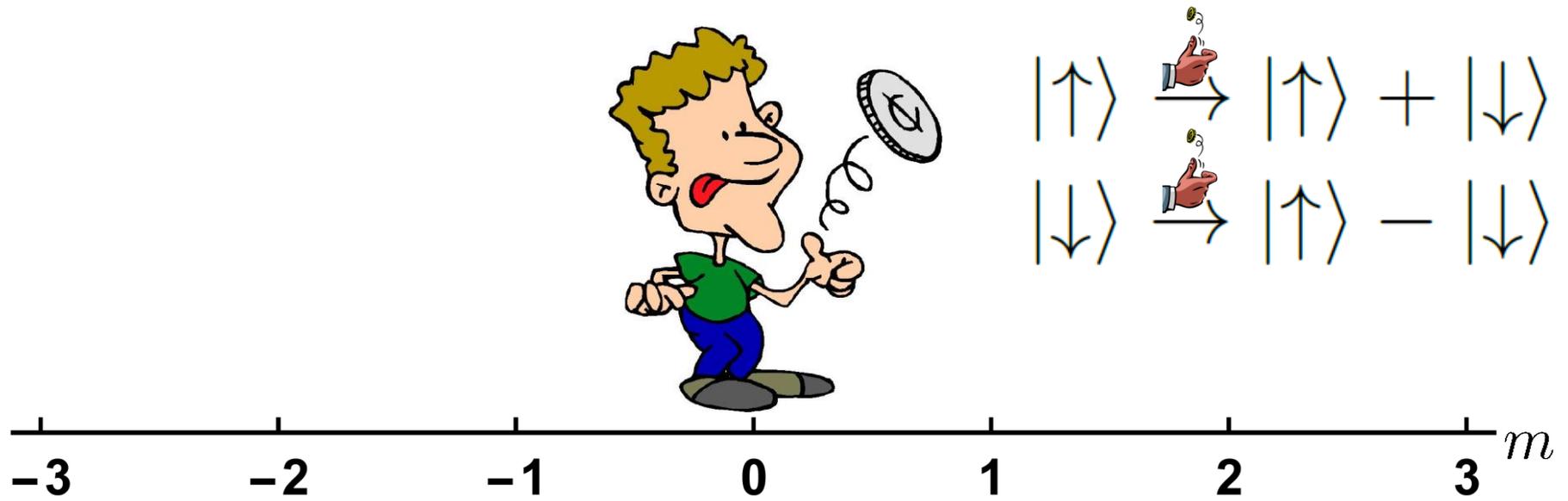
1<sup>st</sup> time step



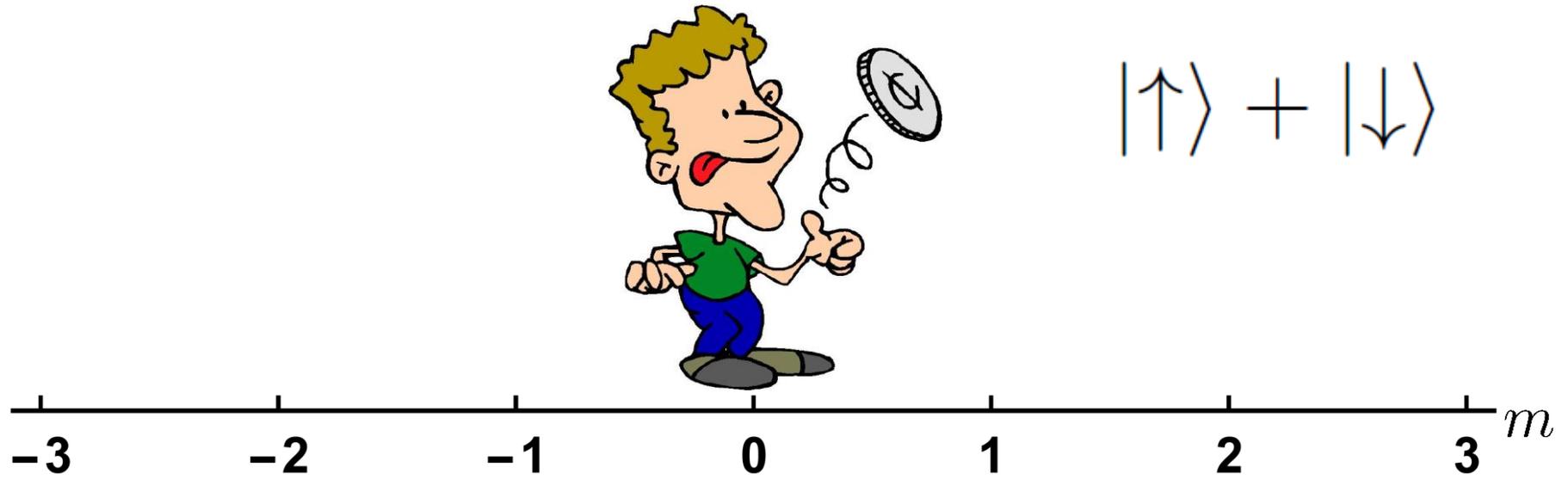
1<sup>st</sup> time step



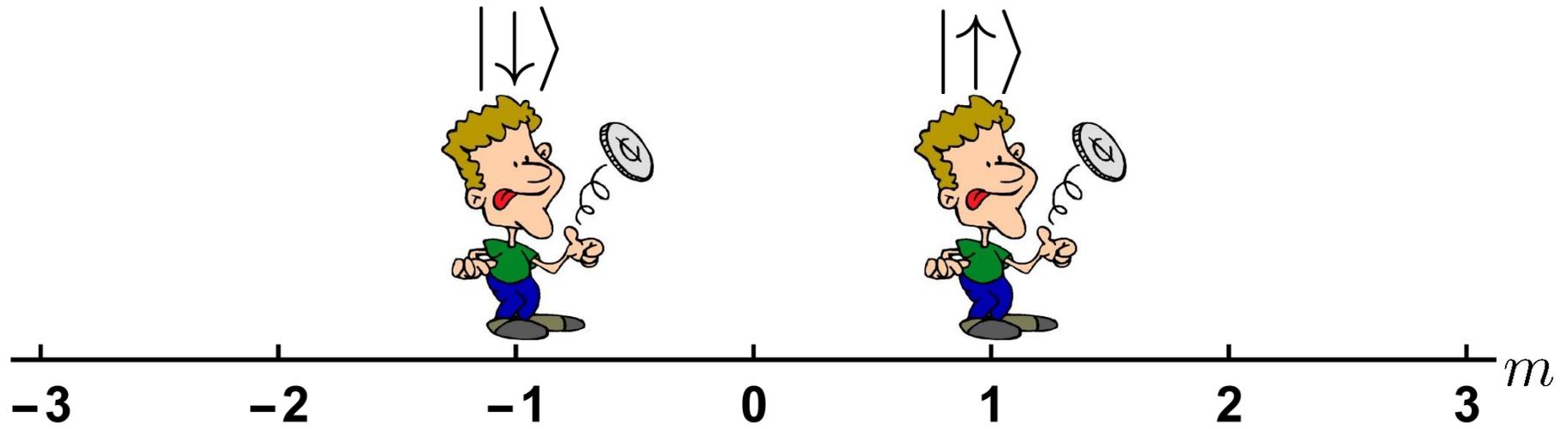
1<sup>st</sup> time step



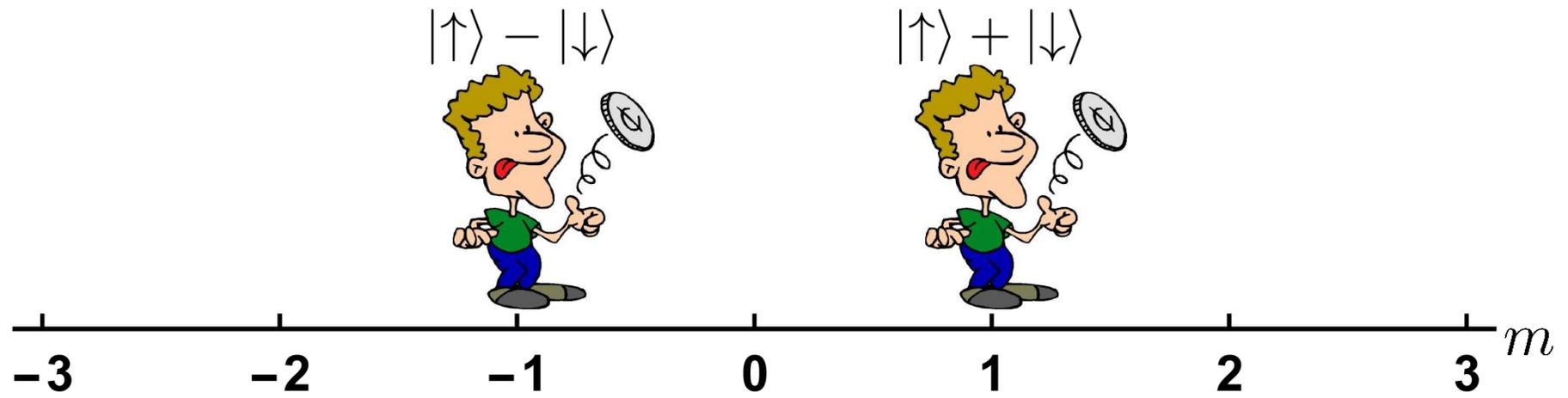
1<sup>st</sup> time step



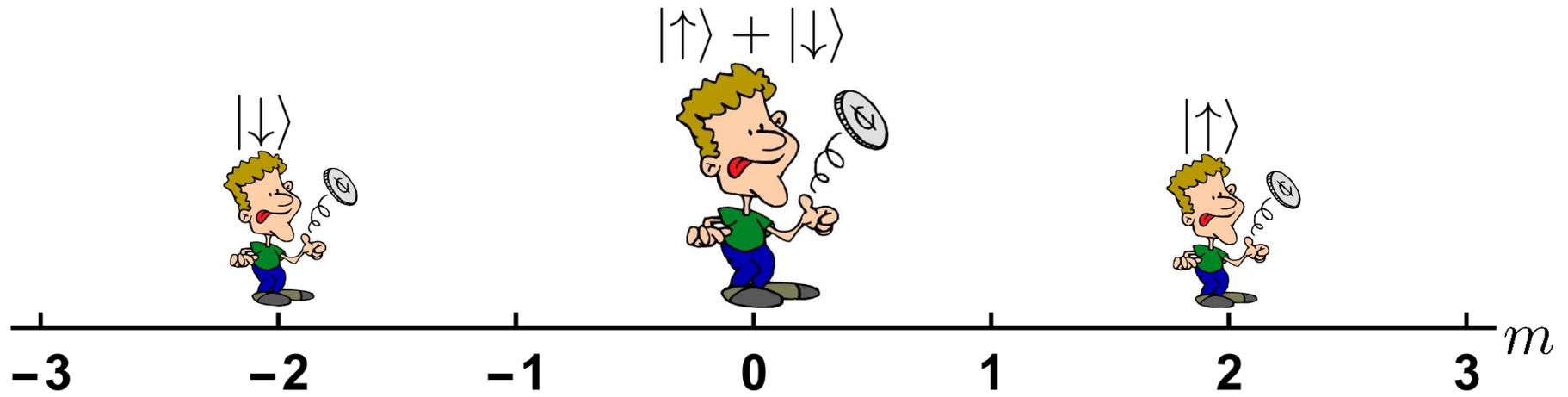
1<sup>st</sup> time step



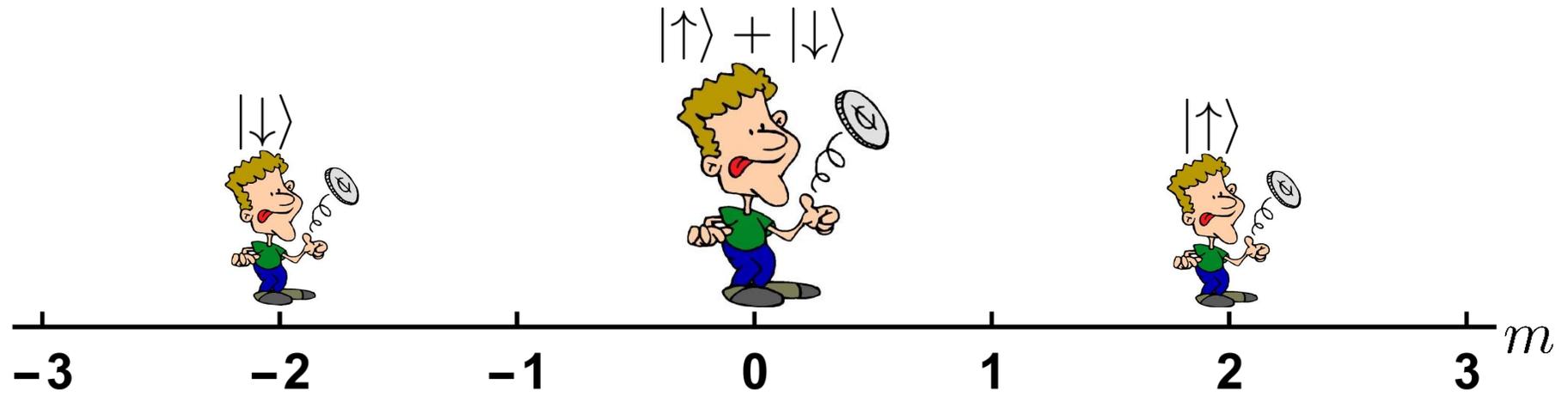
2<sup>nd</sup> time step



2<sup>nd</sup> time step



... and so on!



# Why?



Topological simulator

Quantum search algorithm

Entanglement generator

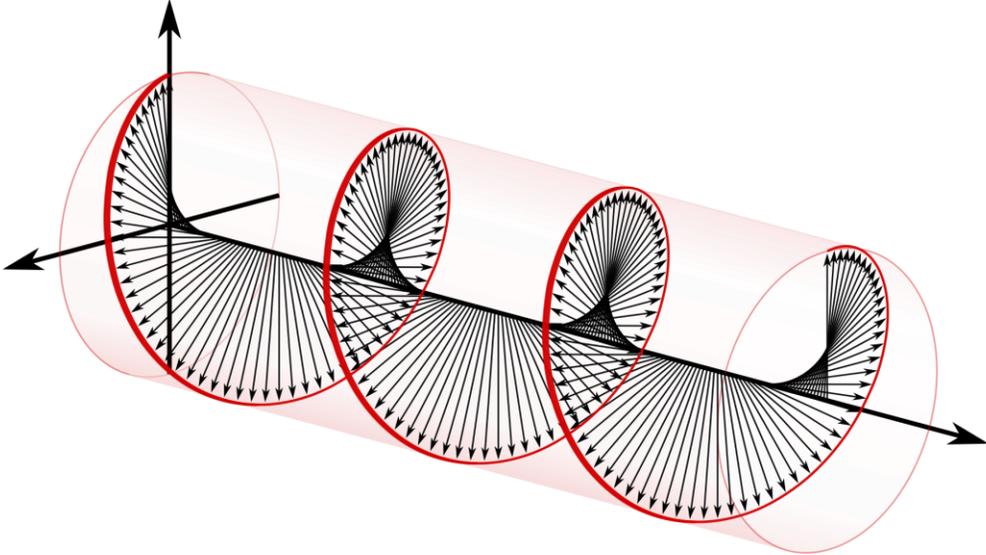
Transport phenomena

# *Photonic quantum walks*

# Photonic quantum walks (coin)



COIN  
 $\{|\uparrow\rangle, |\downarrow\rangle\}$



POLARIZATION  
 $\{|L\rangle, |R\rangle\}$

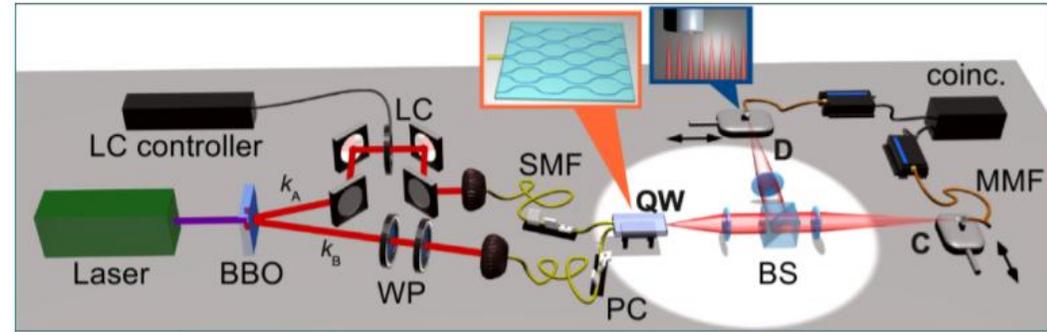
# Photonic quantum walks (walker)



$|m\rangle$

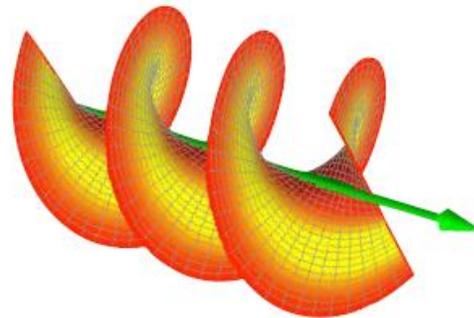


## position modes

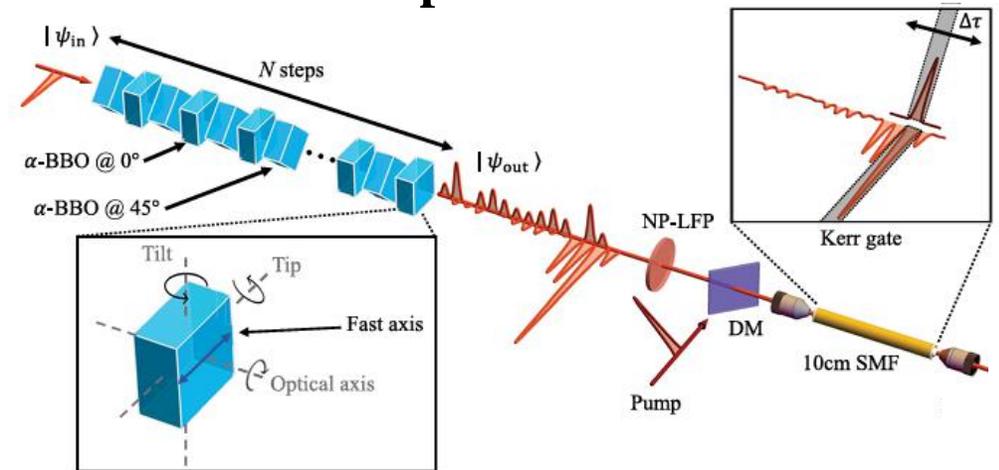


L. Sansoni et al., Phys. Rev. Lett. 108, 010502 (2012)

## helical modes



## temporal modes



K. Fenwick et al., Optica 11, 1017 (2024)

F. Cardano et al., Sci. Adv. 1, e1500087 (2015)

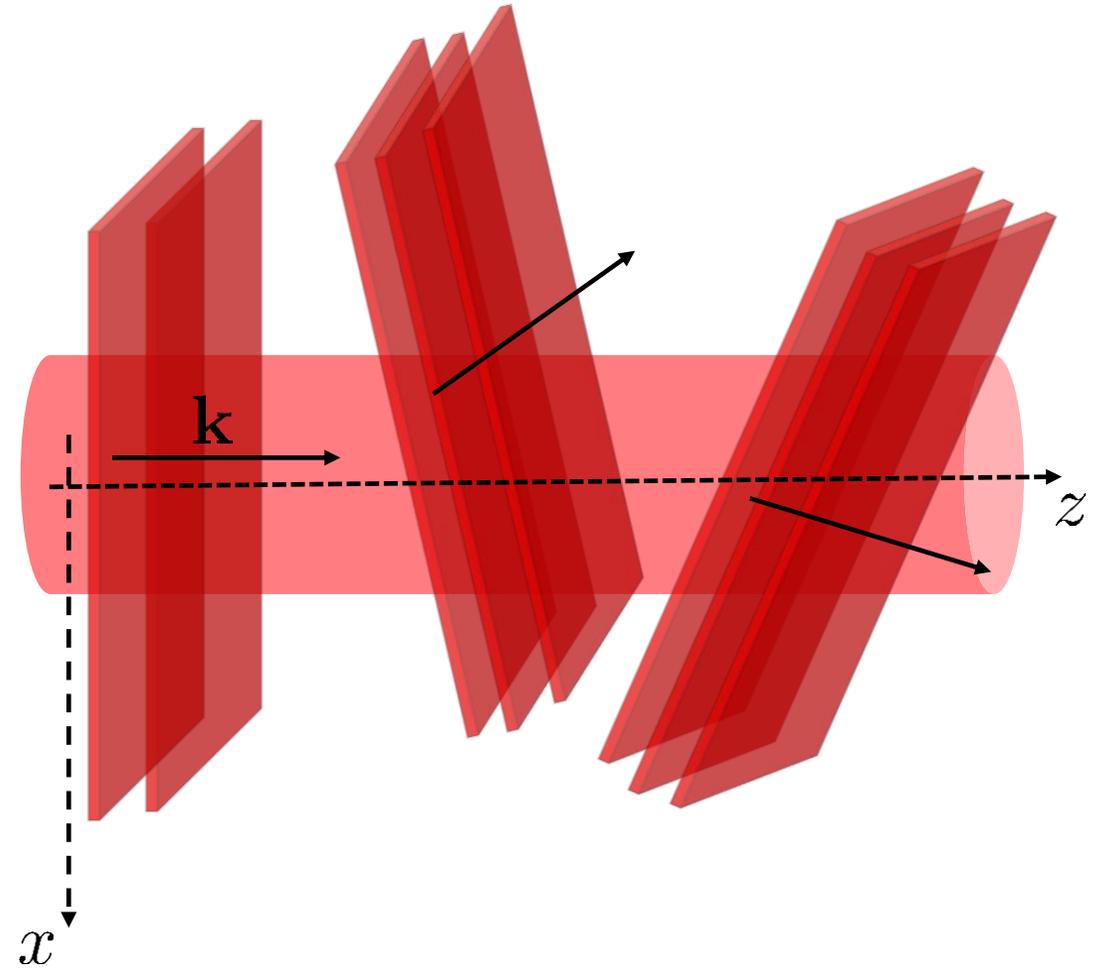
Our walker



$|m\rangle$



**transverse momentum modes**



## Quantizing light transverse momentum

$$E(x, y, z) = E_0(x, y, z)e^{ik_z z} e^{ik_x x}$$

## Quantizing light transverse momentum

$$E(x, y, z) = E_0(x, y, z) e^{ik_z z} e^{im\Delta k_\perp x}$$

$$\Delta k_\perp = \frac{2\pi}{\Lambda} \quad m \in \mathbb{Z}$$

## Quantizing light transverse momentum

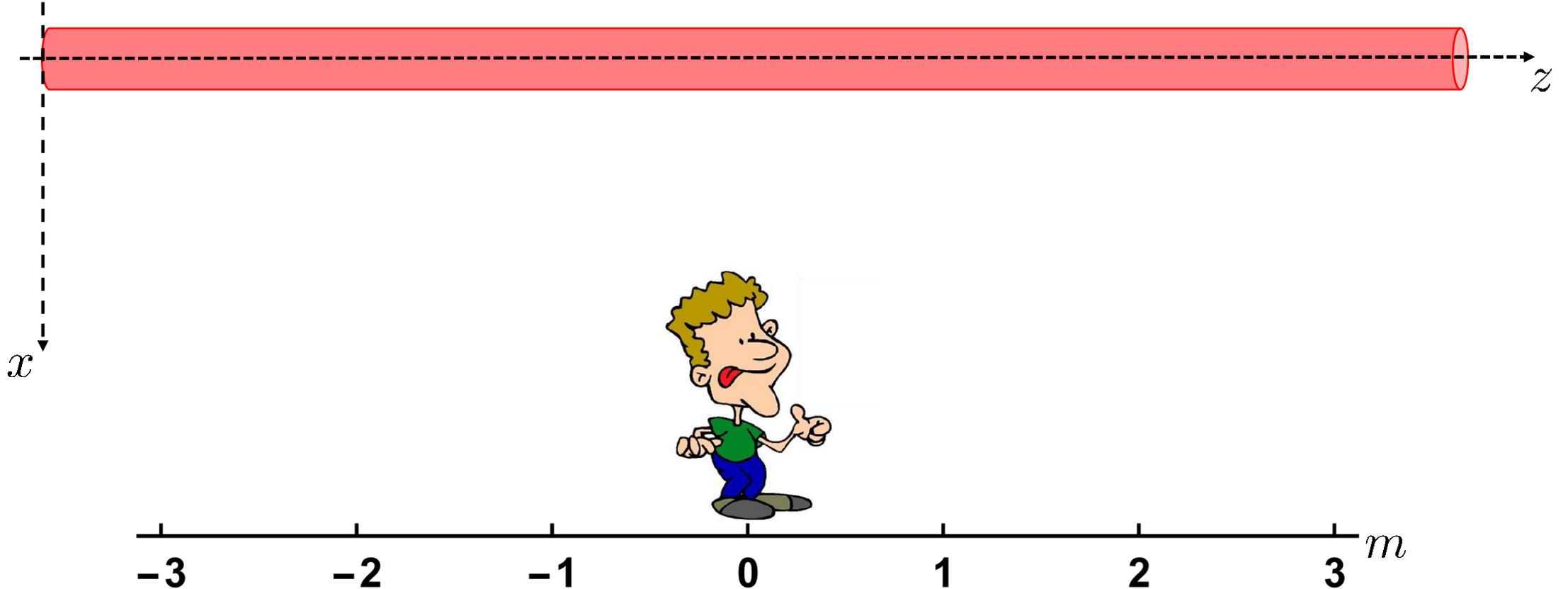
$$|m\rangle = E_0(x, y, z) e^{ik_z z} e^{im\Delta k_\perp x}$$

$$\Delta k_\perp = \frac{2\pi}{\Lambda} \quad m \in \mathbb{Z}$$

# Quantizing light transverse momentum

$$|0\rangle = E_0(x, y, z)e^{ik_z z}$$

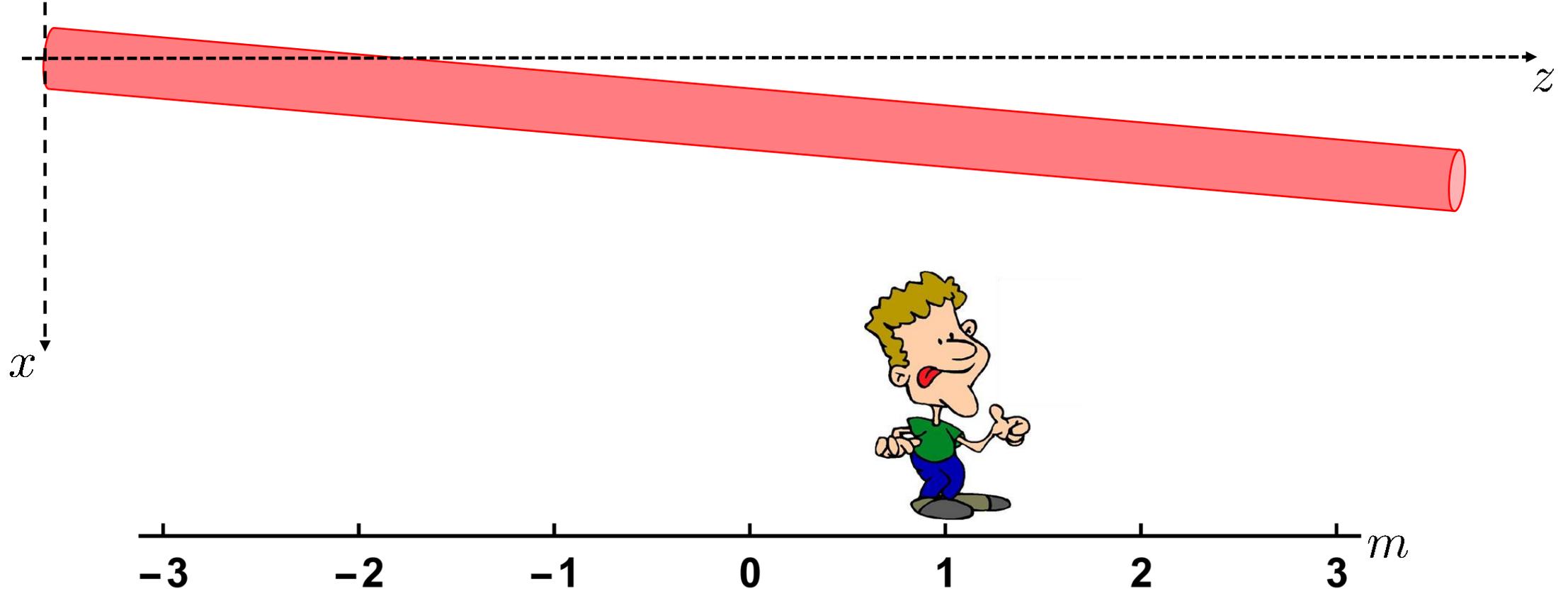
$$\Delta k_{\perp} = \frac{2\pi}{\Lambda} \quad m = 0$$



# Quantizing light transverse momentum

$$|1\rangle = E_0(x, y, z)e^{ik_z z} e^{+i\Delta k_\perp x}$$

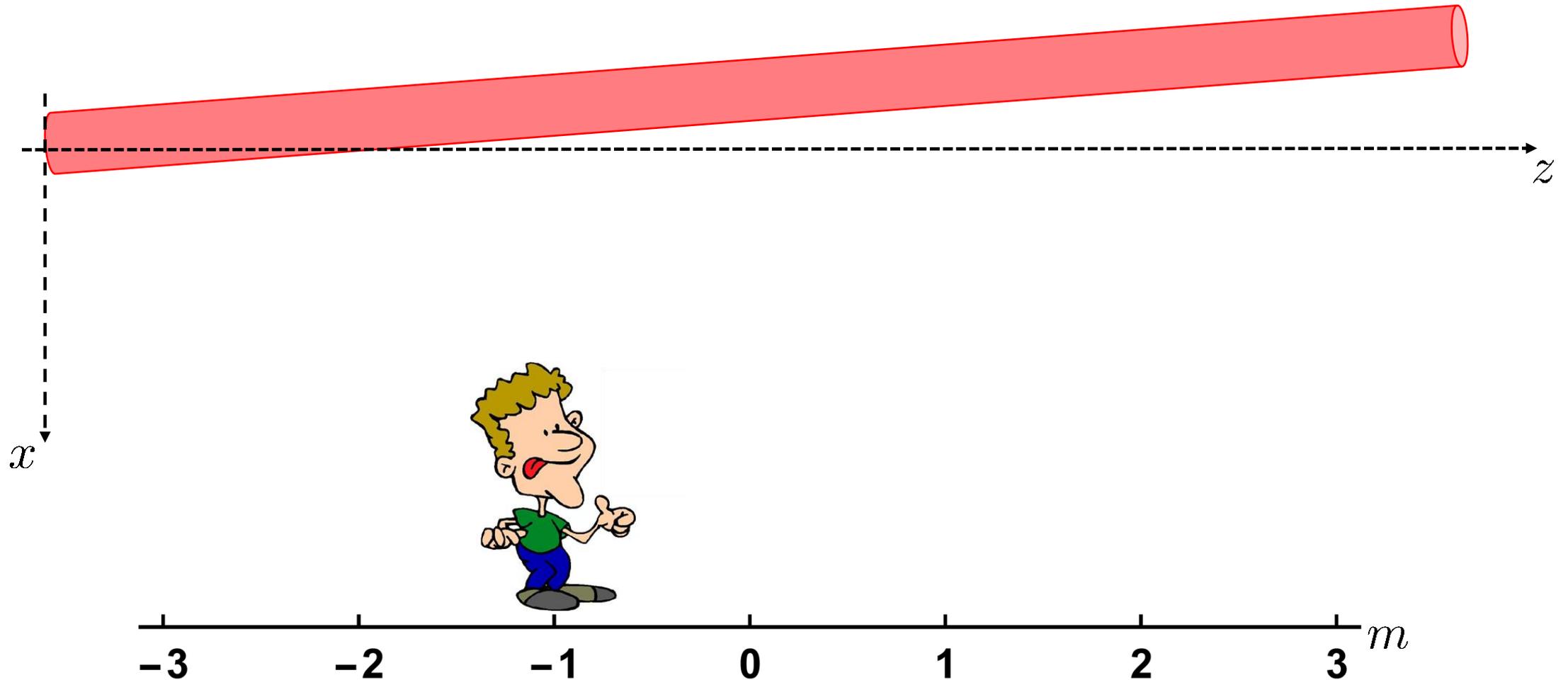
$$\Delta k_\perp = \frac{2\pi}{\Lambda} \quad m = 1$$



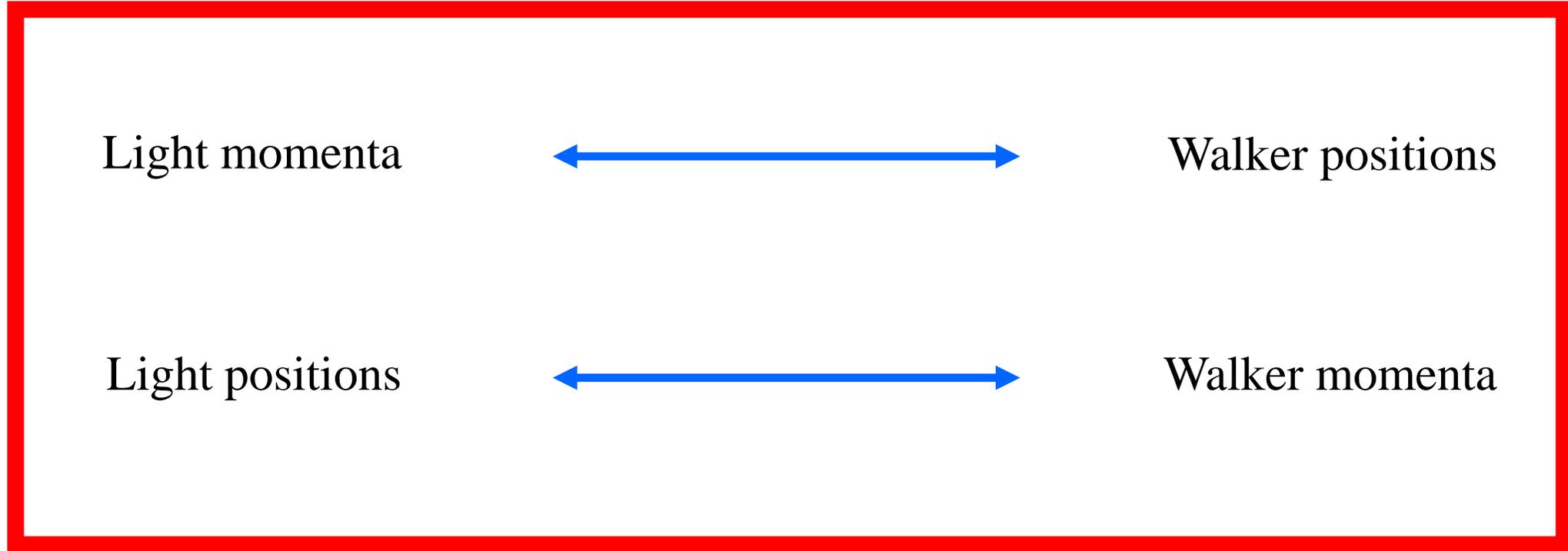
# Quantizing light transverse momentum

$$|-1\rangle = E_0(x, y, z) e^{ik_z z} e^{-i\Delta k_\perp x}$$

$$\Delta k_\perp = \frac{2\pi}{\Lambda} \quad m = -1$$



Keep in mind



Talk by Alessio D'Errico (Tomorrow, 9.30)

Talk by Farid Ghobadi (Thursday, 15:40)

Poster by Maria Gorizia Ammendola (Tomorrow, 16:00-18:00)

# Photonic implementation of the QW dynamics

Waveplate operator

$$L_{\delta}(\theta) = \begin{pmatrix} \cos(\delta/2) & i \sin(\delta/2) e^{-2i\theta} \\ i \sin(\delta/2) e^{2i\theta} & \cos(\delta/2) \end{pmatrix}$$

optical retardation  
(birefringence)

optic-axis orientation

## Coin rotation

$$W = L_{\pi/2}(0) = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & i \\ i & 1 \end{pmatrix} \quad \text{quarter-wave plate}$$

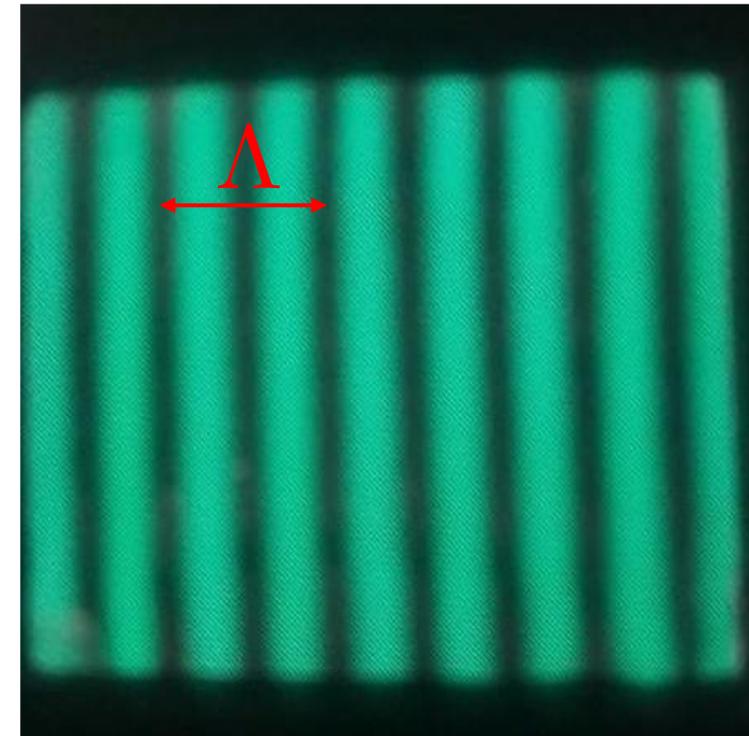
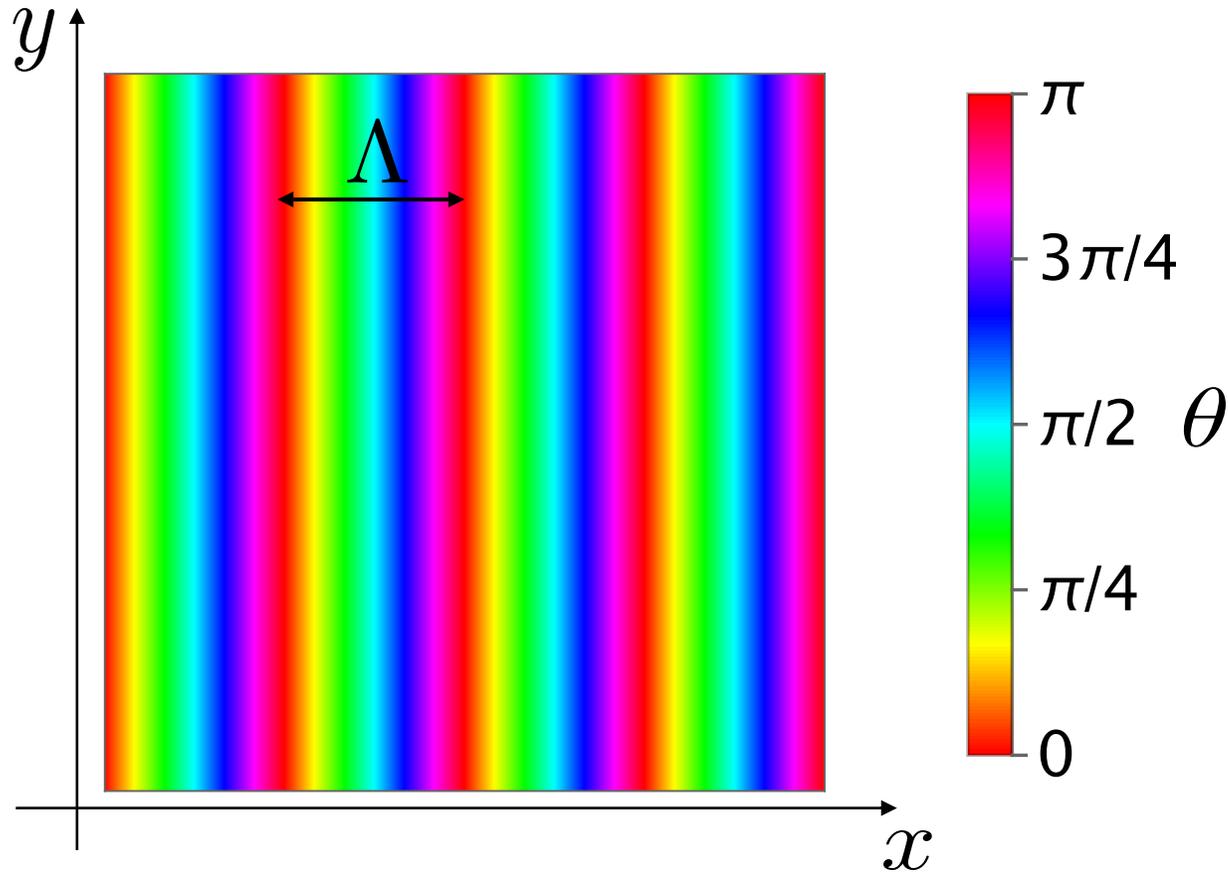
## Coin-dependent translation

$$T_\delta = L_\delta(\theta(x)) = \begin{pmatrix} \cos(\delta/2) & i \sin(\delta/2) e^{-2i\theta(x)} \\ i \sin(\delta/2) e^{2i\theta(x)} & \cos(\delta/2) \end{pmatrix}$$

$$\theta(x) = \frac{\pi}{\Lambda} x \quad \text{g-plate}$$

# Liquid-crystal metasurfaces

$$\theta(x, y) = \theta_0 + \frac{\pi}{\Lambda} x \quad \text{g-plate}$$



$\delta$  electrically tuned

# *Optimizing photonic simulations*

## Standard approach

$$|\psi_\tau\rangle = U^\tau |\psi_0\rangle = UUU\dots UU |\psi_0\rangle$$

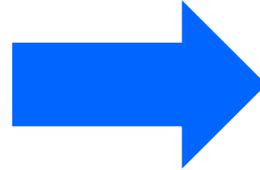


Rotation + Translation  
(or a combination of them)

## Standard approach

$$|\psi_\tau\rangle = U^\tau |\psi_0\rangle = UUU\dots UU |\psi_0\rangle$$

Rotation + Translation  
(or a combination of them)

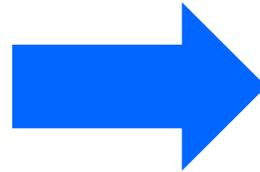


(at least) 2 optical elements  
for each time step

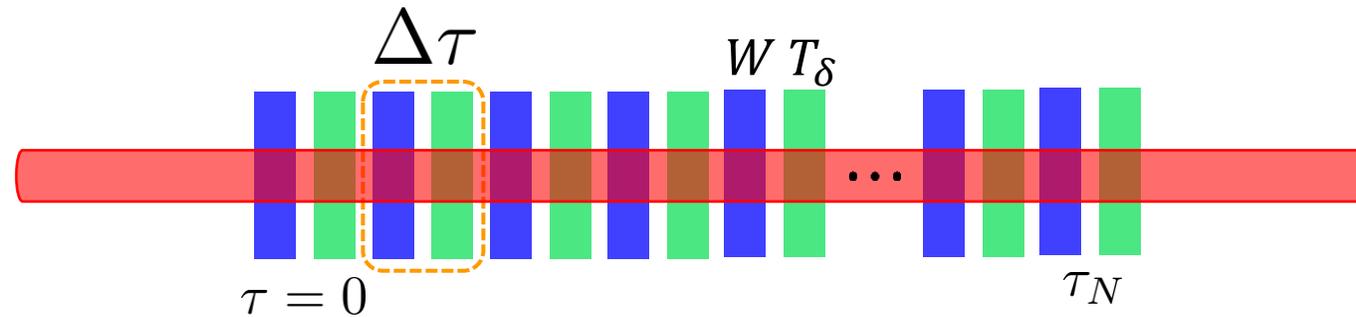
# Standard approach

$$|\psi_\tau\rangle = U^\tau |\psi_0\rangle = UUU\dots UU |\psi_0\rangle$$

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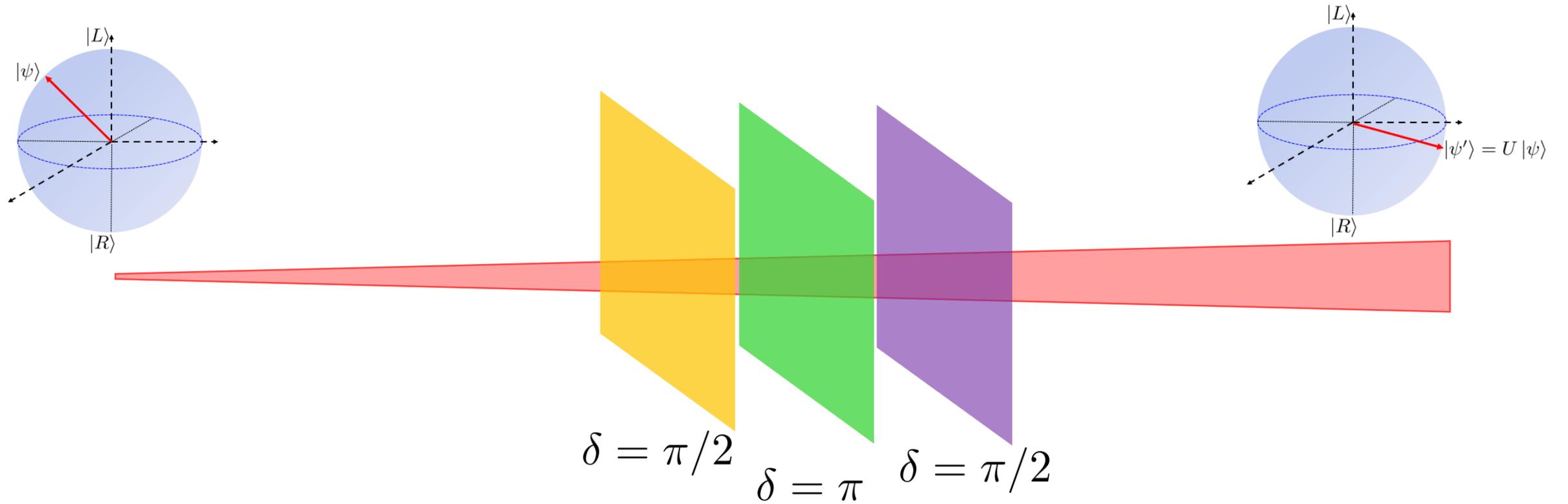


$$|\psi_\tau\rangle = \prod_{i=1}^{\tau} \left[ \begin{pmatrix} \cos \frac{\delta}{2} & i \sin \frac{\delta}{2} e^{-2i\frac{\pi}{\Lambda}x} \\ i \sin \frac{\delta}{2} e^{+2i\frac{\pi}{\Lambda}x} & \cos \frac{\delta}{2} \end{pmatrix} \begin{pmatrix} \frac{1}{\sqrt{2}} & \frac{i}{\sqrt{2}} \\ \frac{i}{\sqrt{2}} & \frac{1}{\sqrt{2}} \end{pmatrix} \right] |\psi_0\rangle$$

$$|\psi_\tau\rangle = \begin{pmatrix} \alpha(x) & -\beta(x) \\ \beta^*(x) & \alpha^*(x) \end{pmatrix} |\psi_0\rangle$$

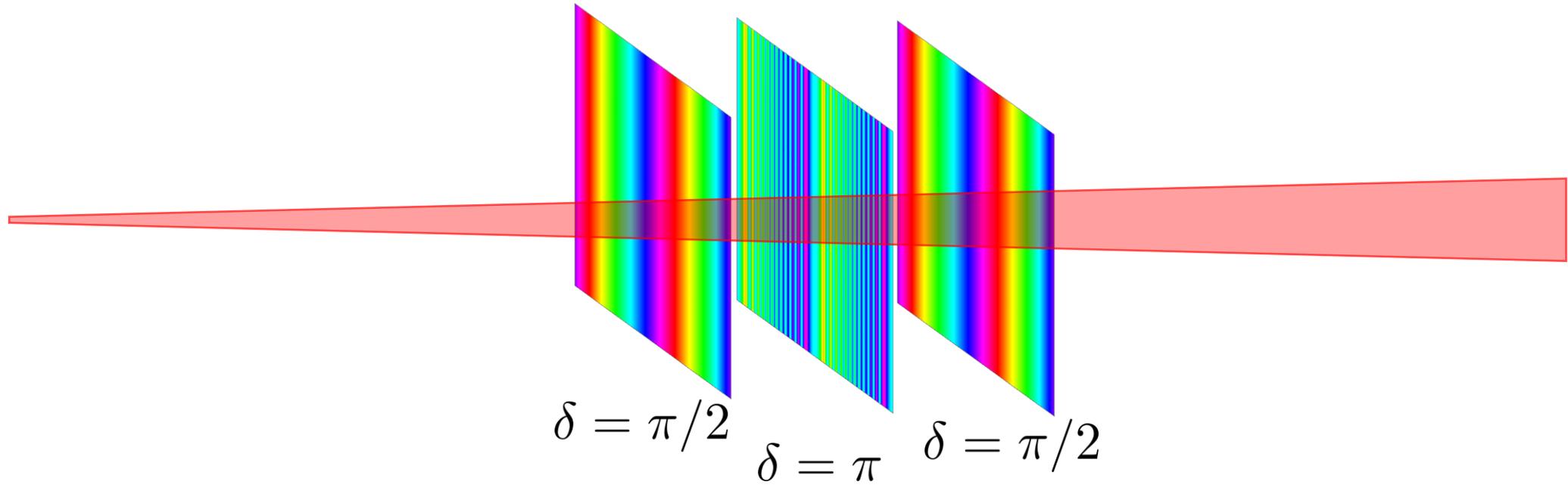
Position-dependent polarization rotation

# Uniform polarization rotation $U$



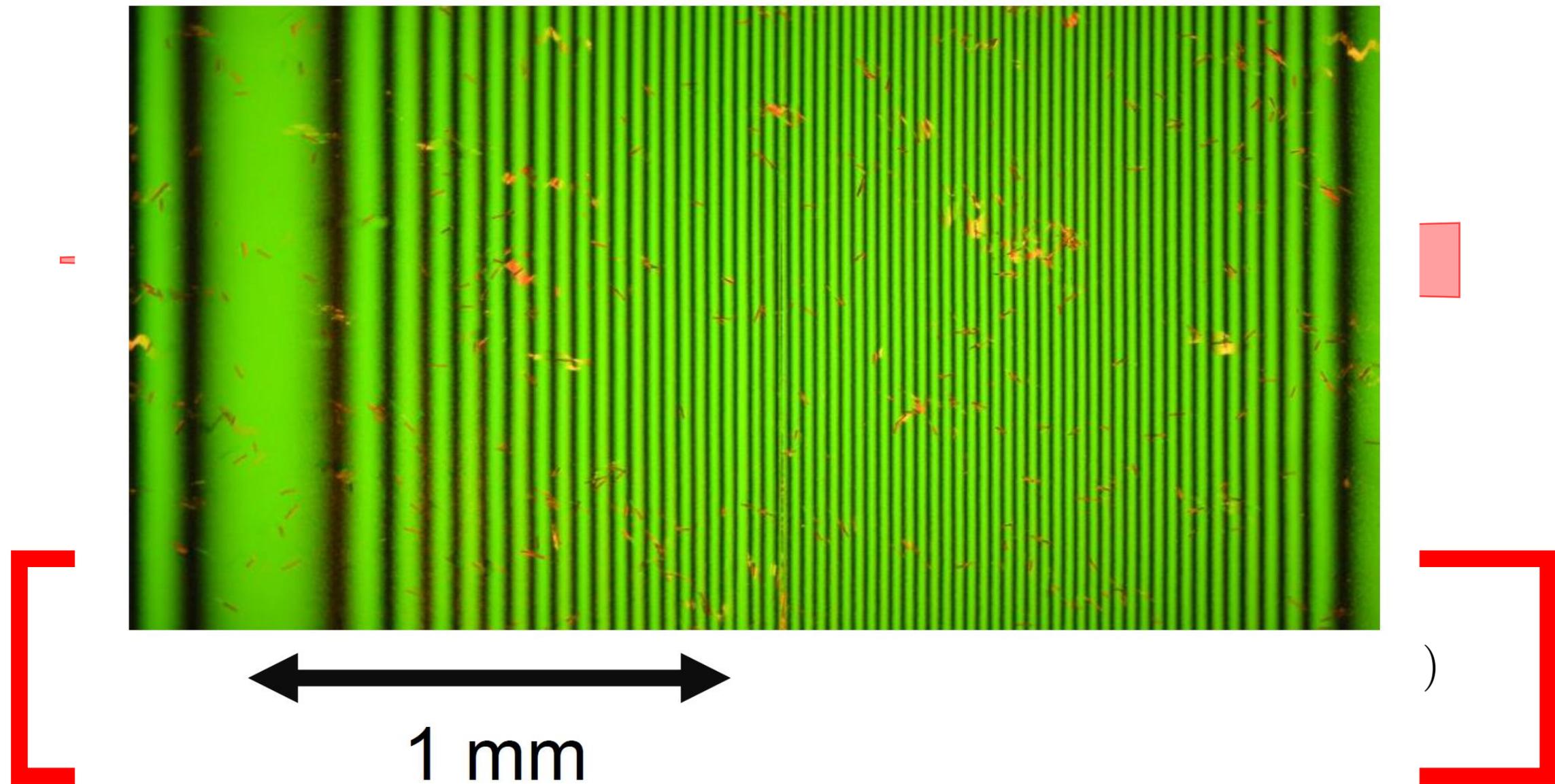
$$U = L_{\pi/2}(\theta_1)L_{\pi}(\theta_2)L_{\pi/2}(\theta_3) \equiv \mathcal{L}(\theta_1, \theta_2, \theta_3)$$

# Non-Uniform polarization rotation $U(x)$



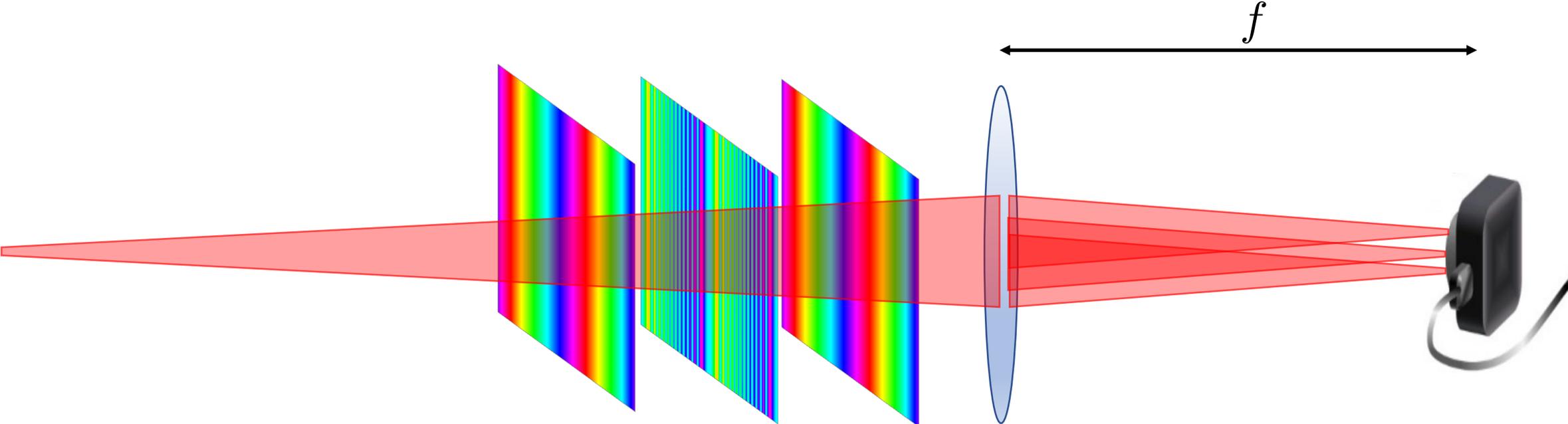
$$U(x) = L_{\pi/2}(\theta_1(x))L_{\pi}(\theta_2(x))L_{\pi/2}(\theta_3(x)) \equiv \mathcal{L}(\theta_1(x), \theta_2(x), \theta_3(x))$$

# Non-Uniform polarization rotation $U(x)$

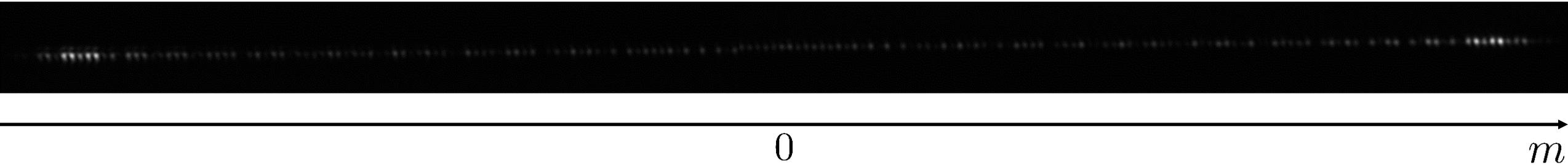
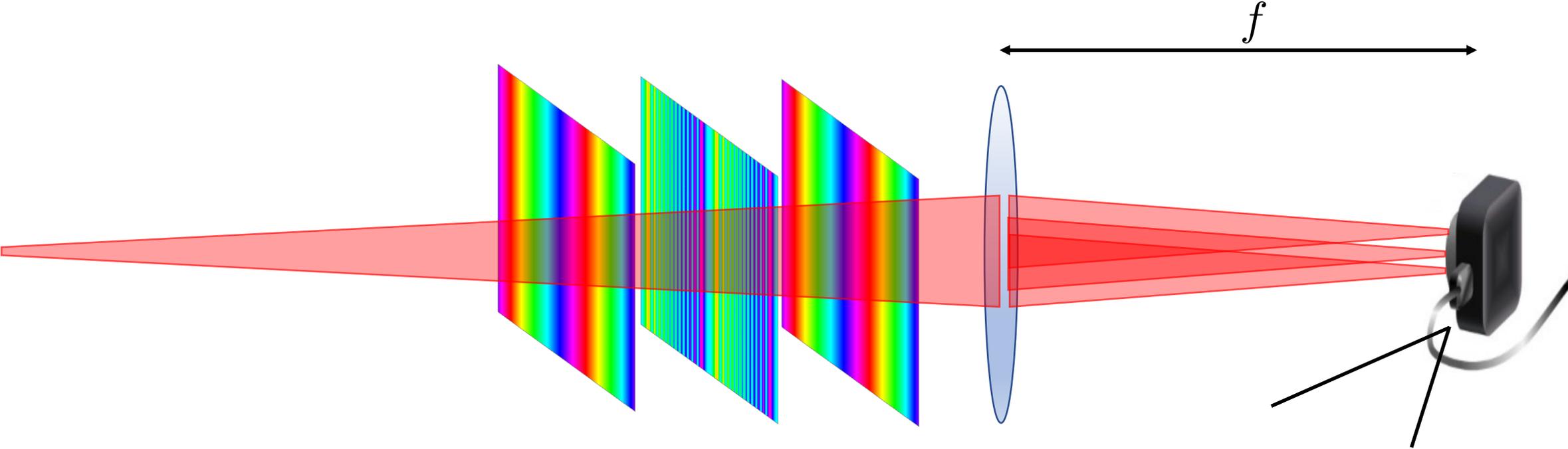


# *Ultra-long quantum walks*

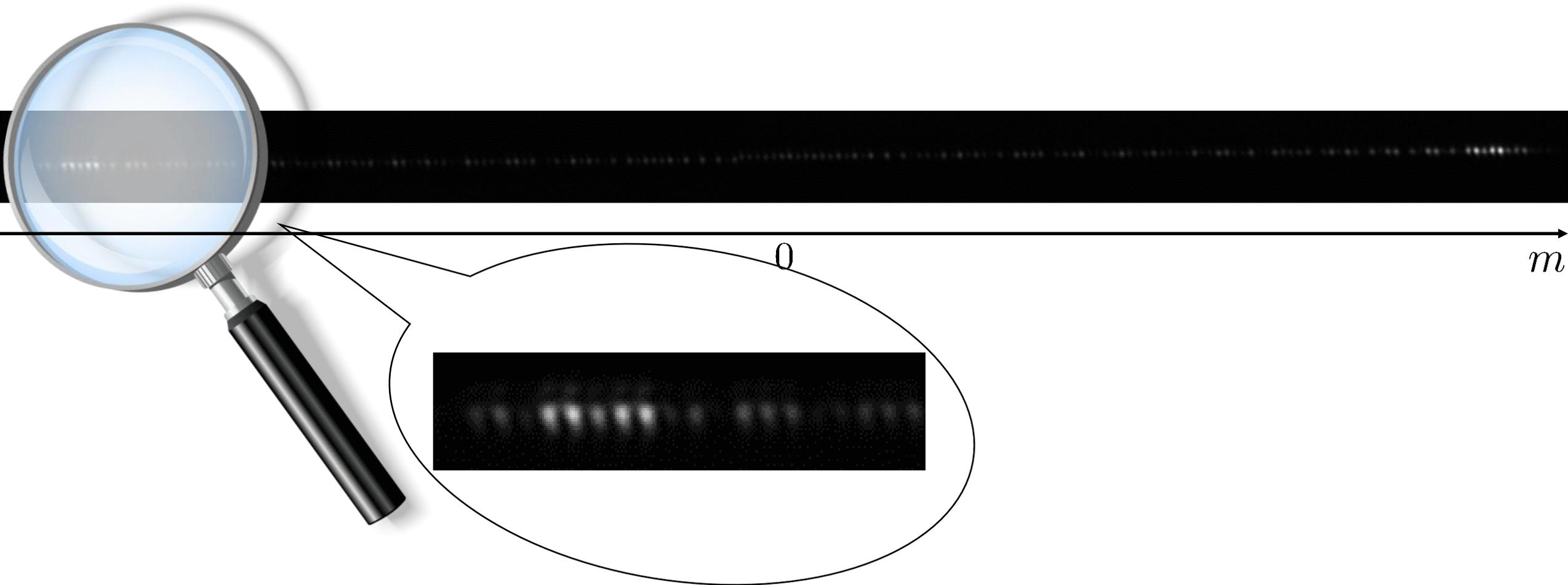
# 240-step quantum walk



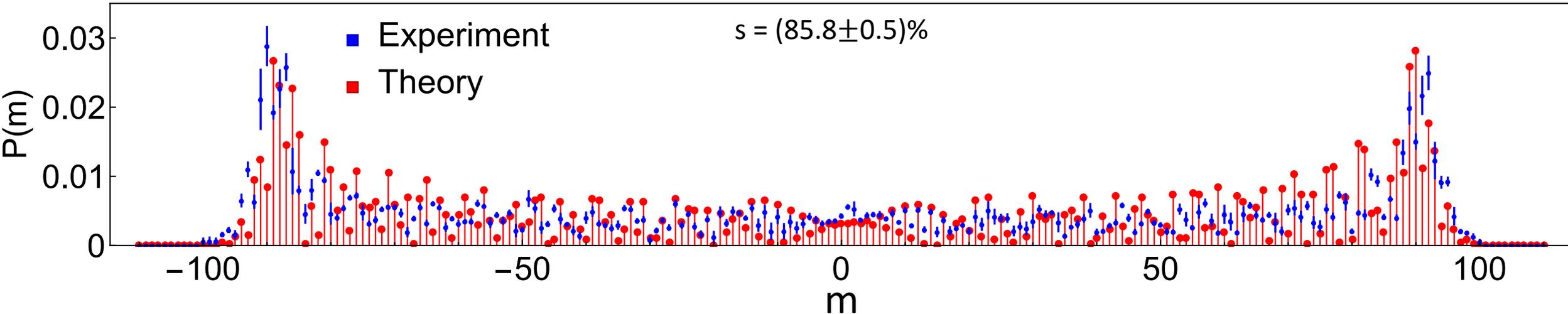
# 240-step quantum walk



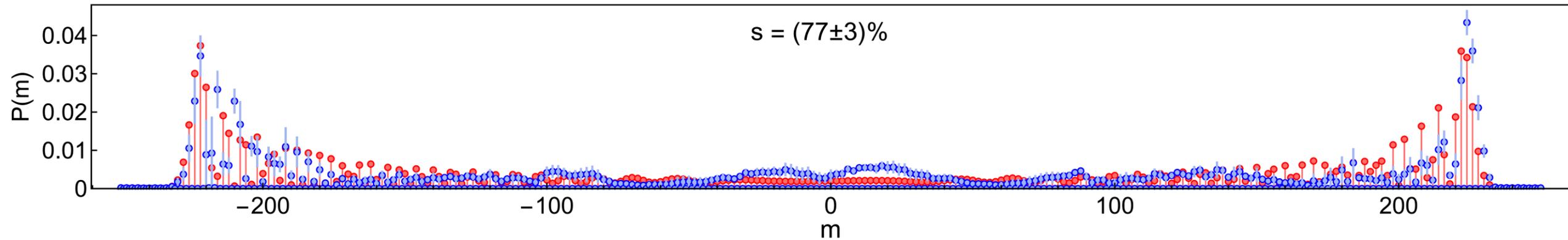
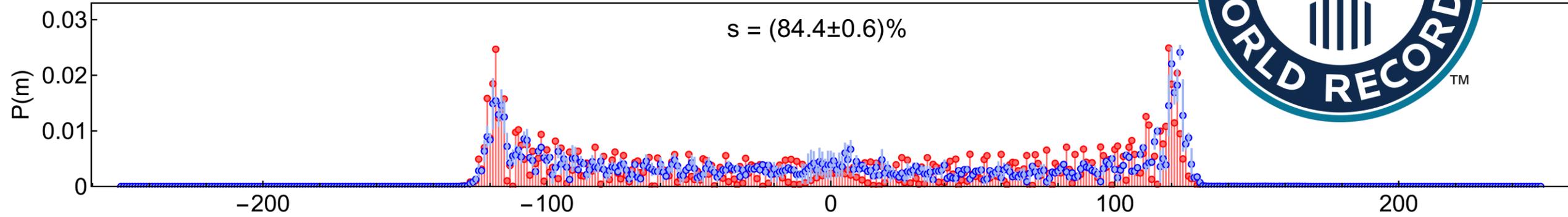
# 240-step quantum walk



# 240-step quantum walk

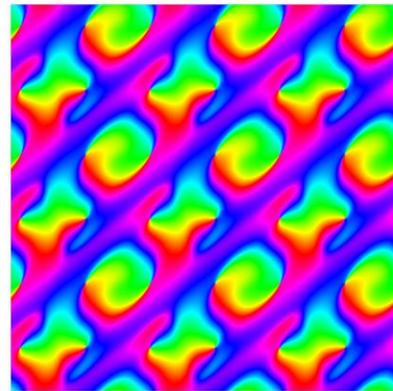
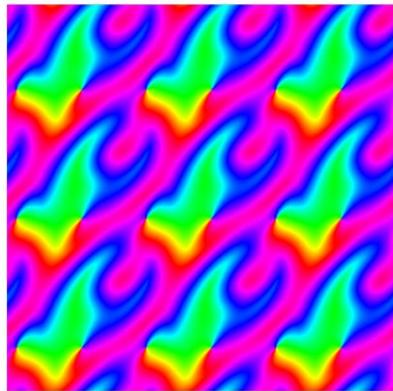
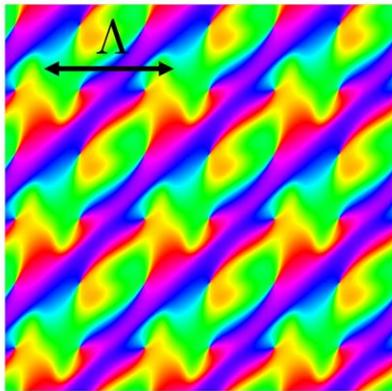
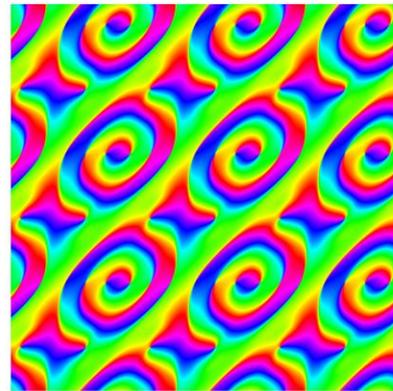
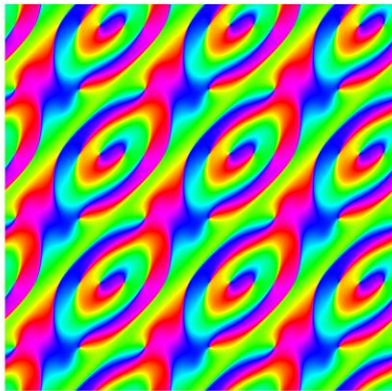
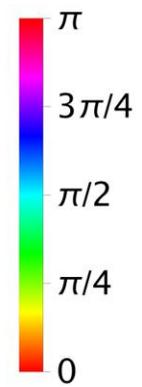
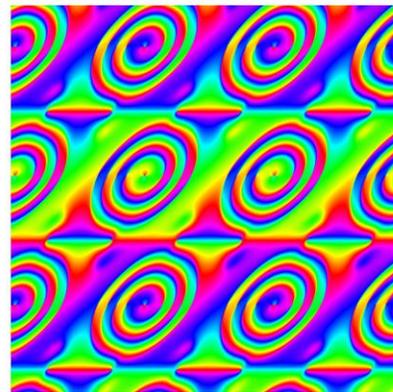
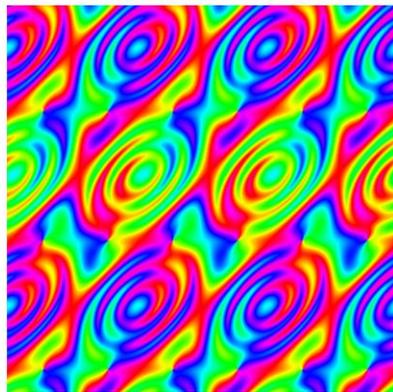
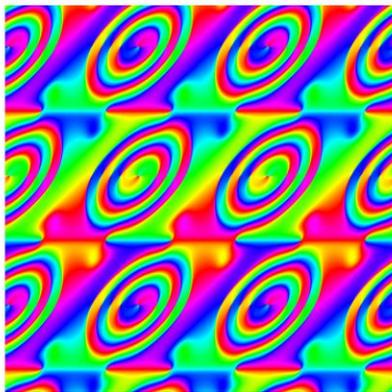


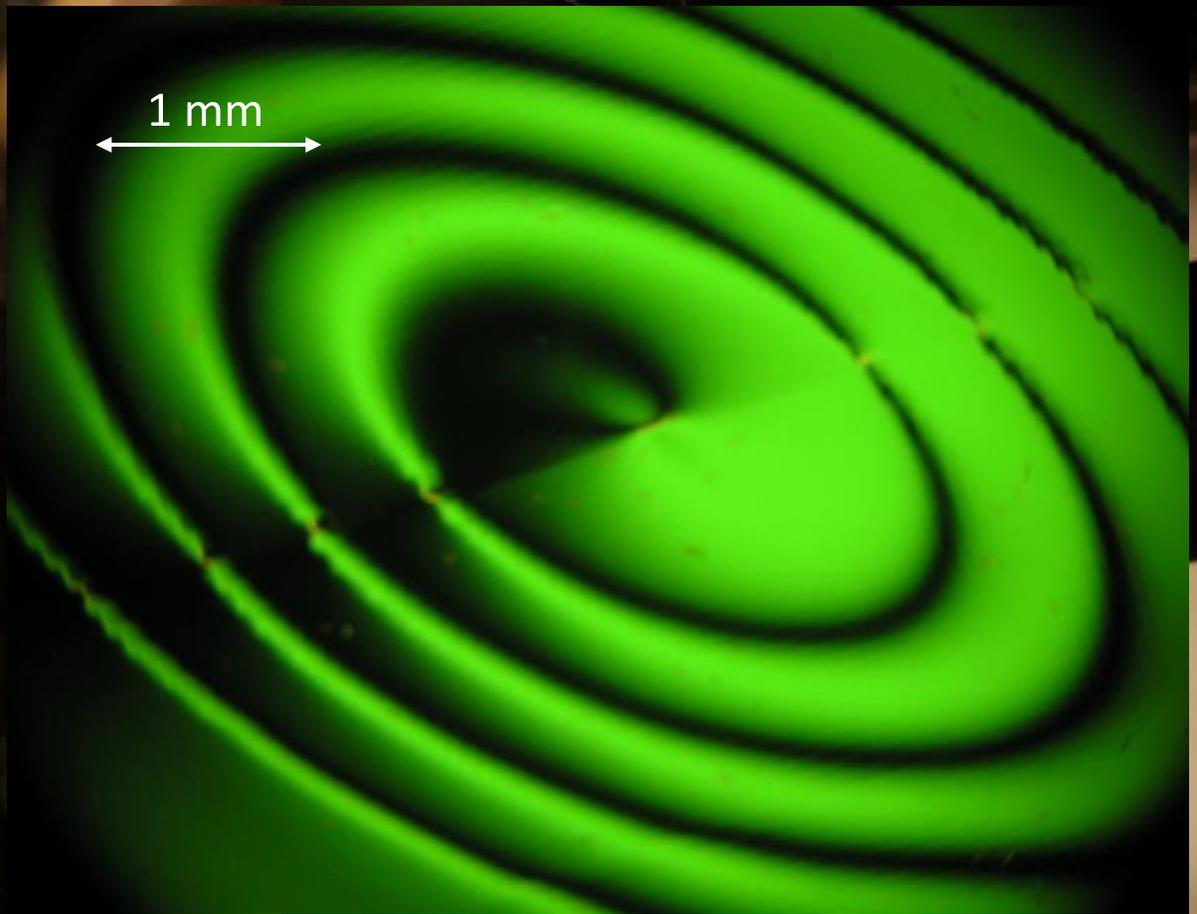
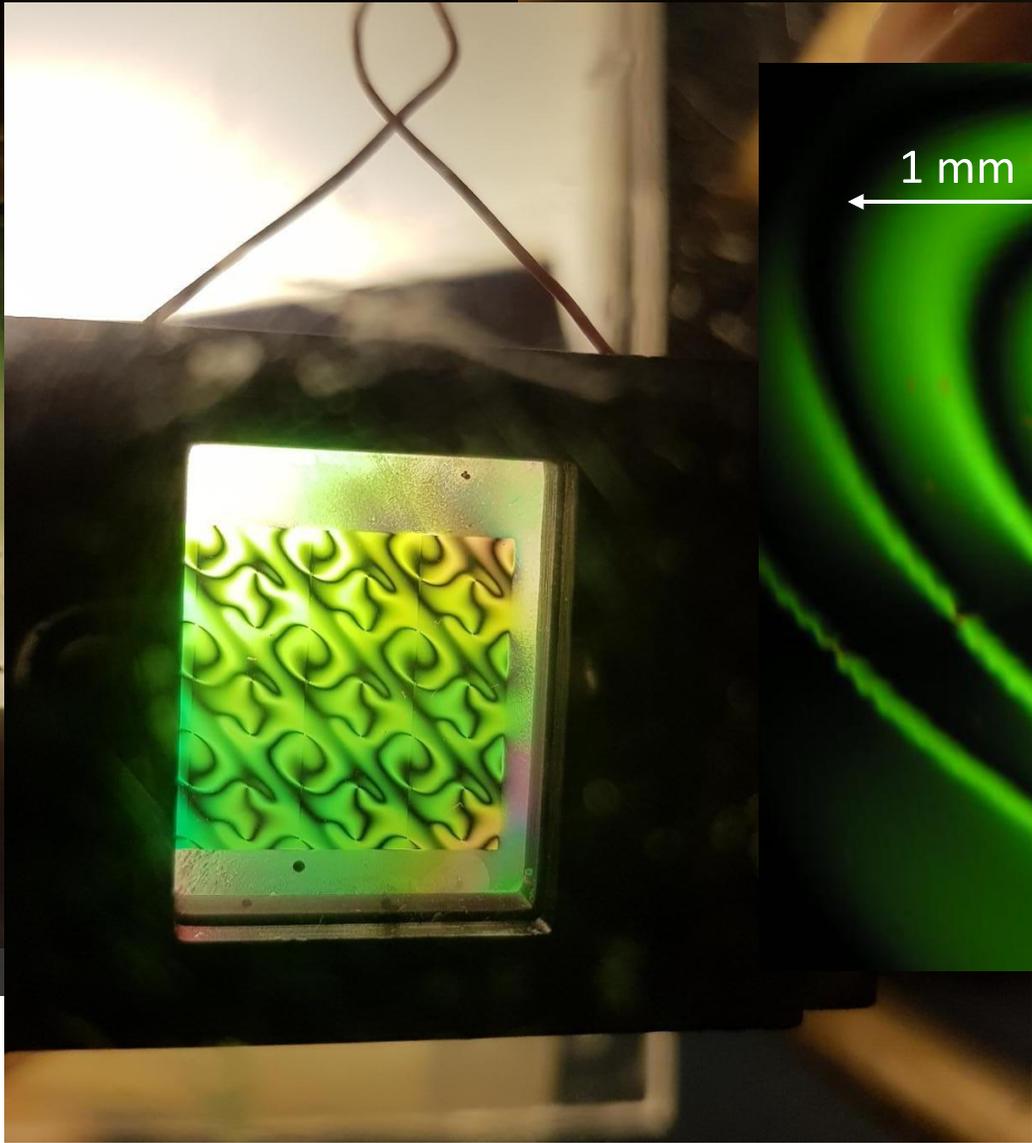
# 320-step quantum walk (160+160)

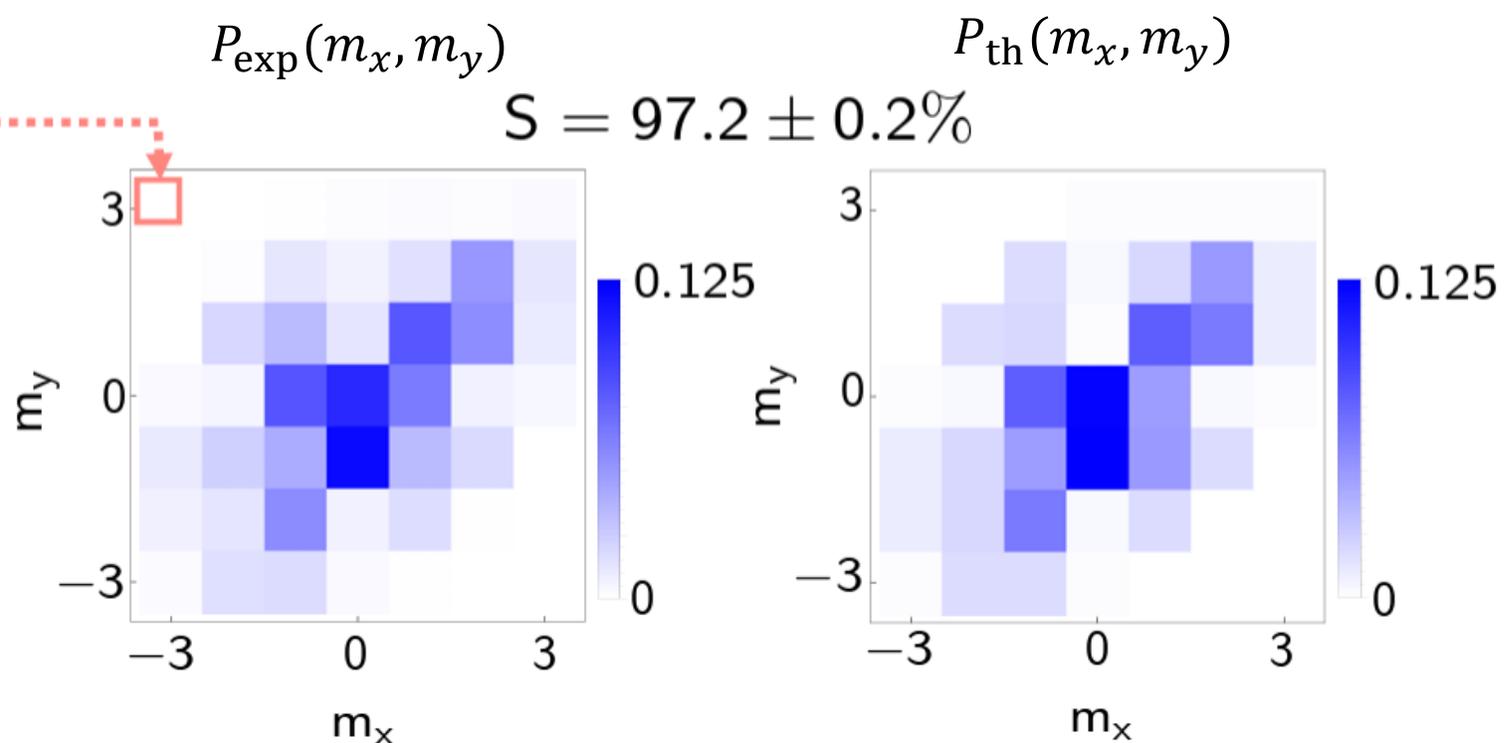
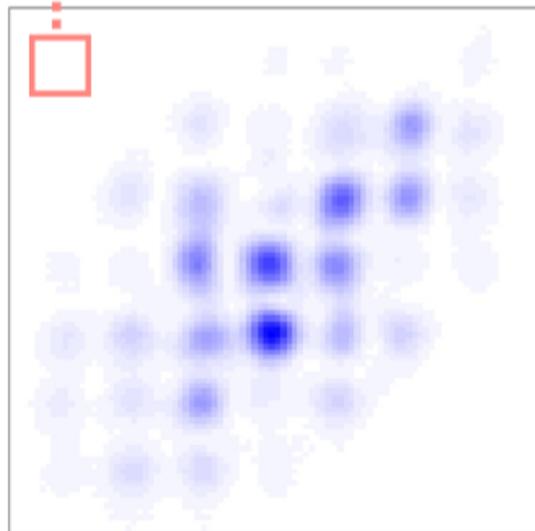
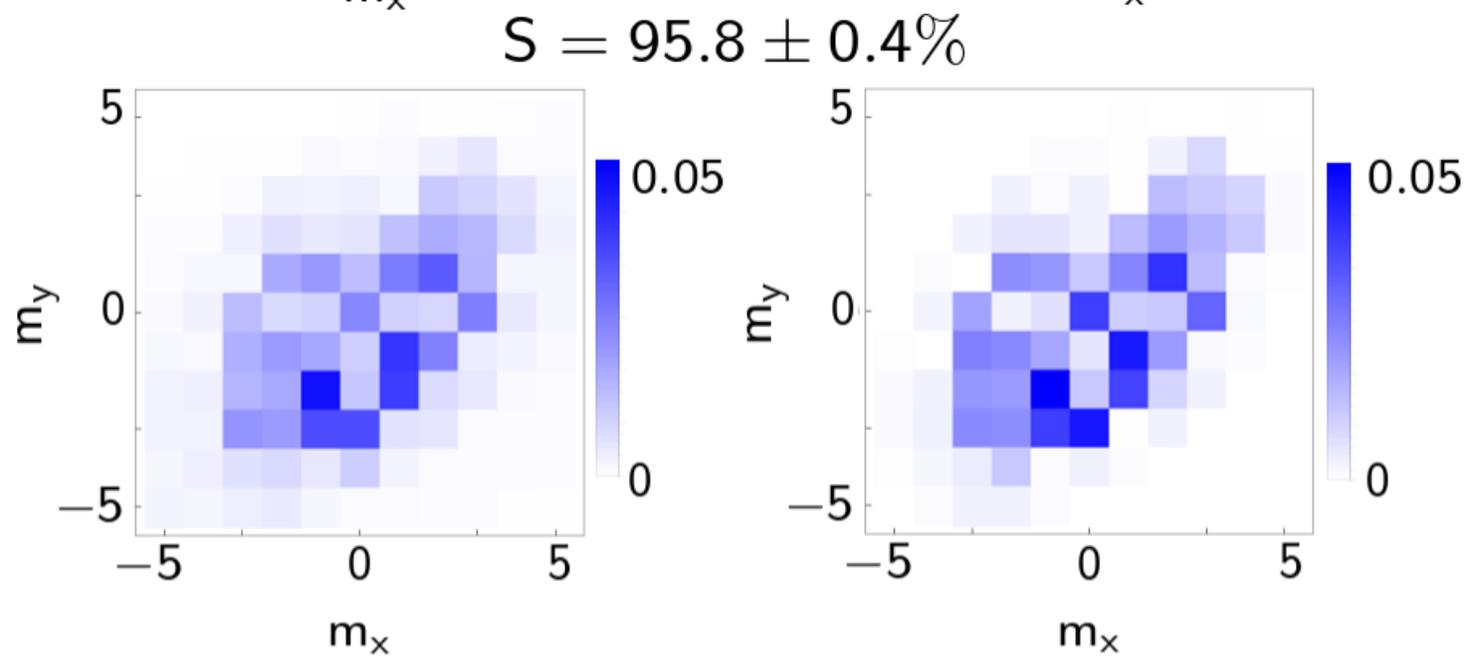
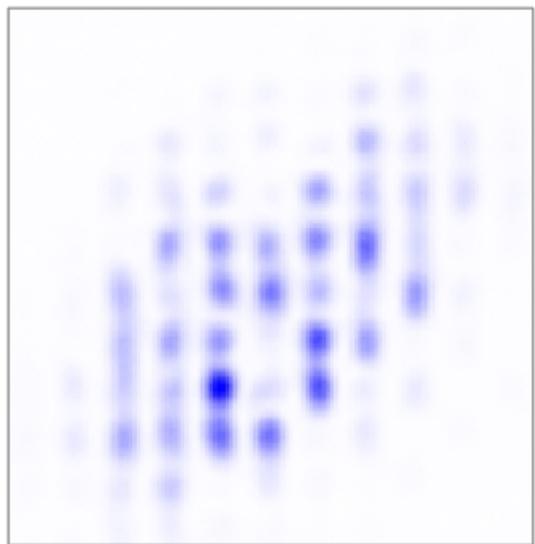


# *Large-scale 2D quantum walks*

M.G. Ammendola et al., arXiv:2406.08652  
Advanced Photonics (*in press*)

$\theta_1(x, y)$  $\theta_2(x, y)$  $\theta_3(x, y)$  $\tau = 3$  $\tau = 5$  $\tau = 10$ 



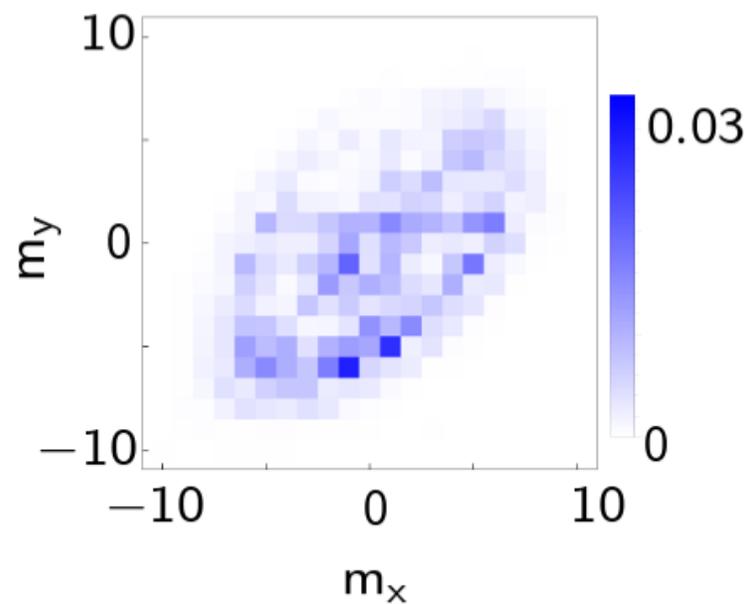
$\tau = 3$  $\tau = 5$ 

$\tau = 10$

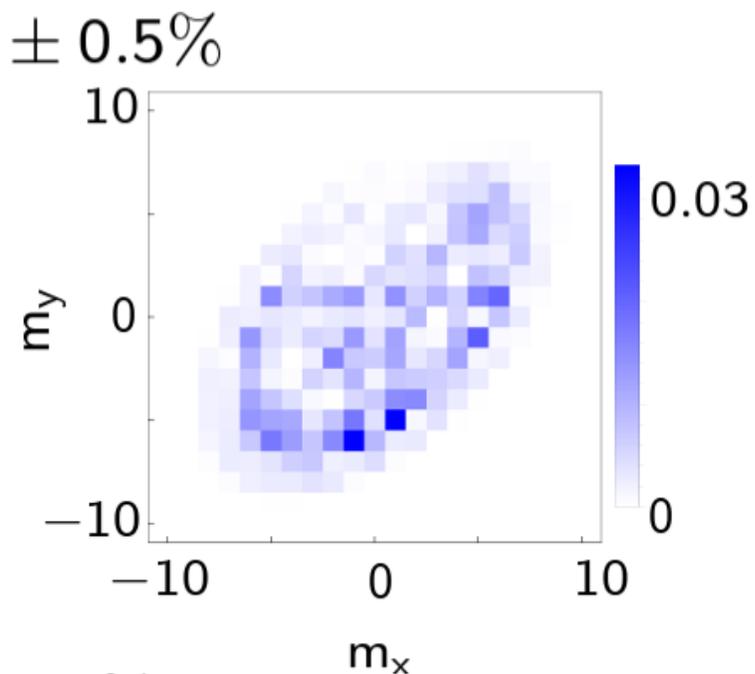


$P_{\text{exp}}(m_x, m_y)$

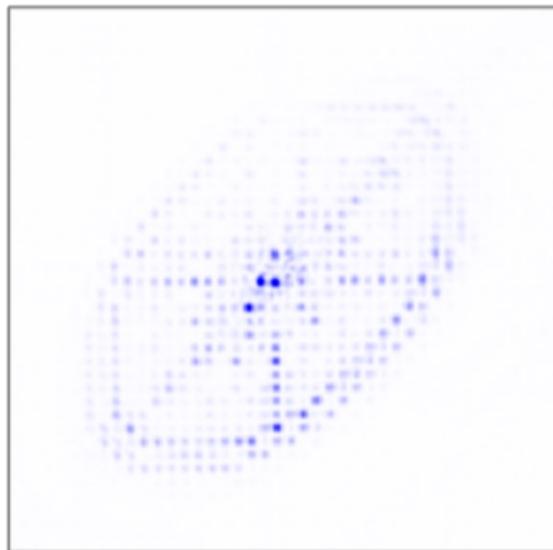
$S = 95.8 \pm 0.5\%$



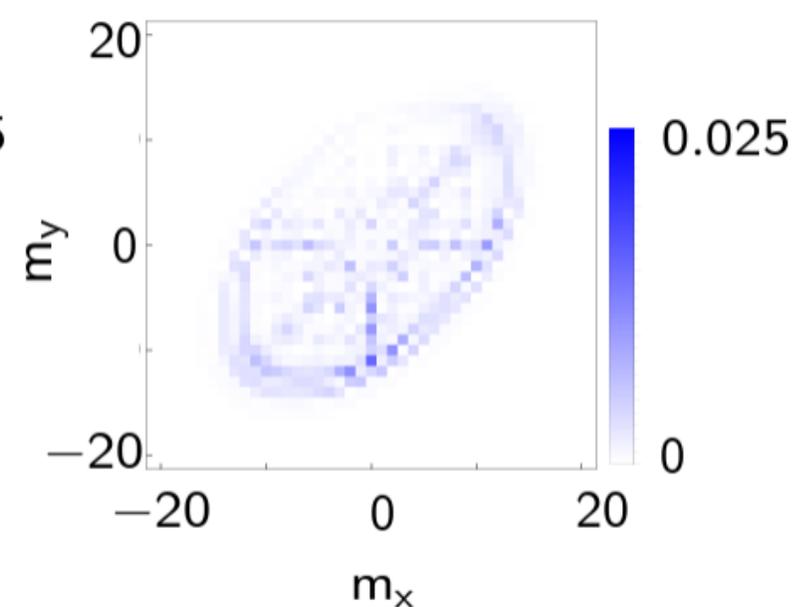
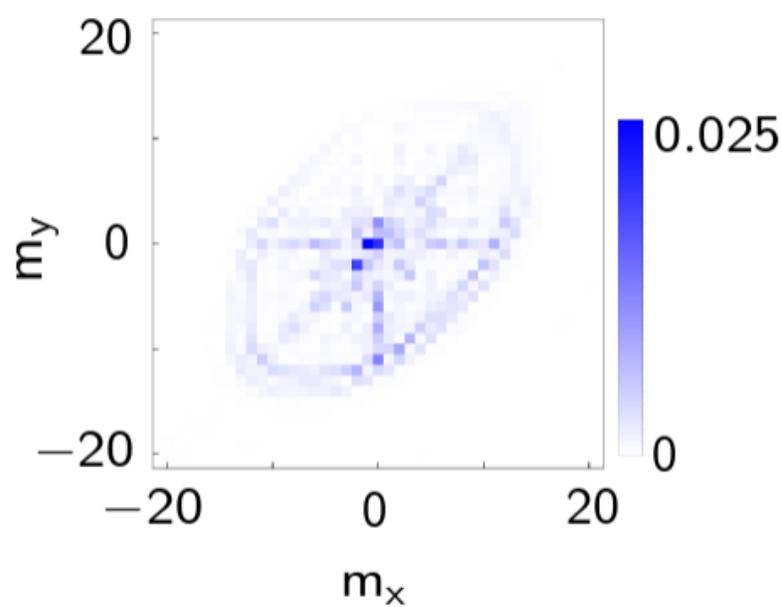
$P_{\text{th}}(m_x, m_y)$



$\tau = 20$



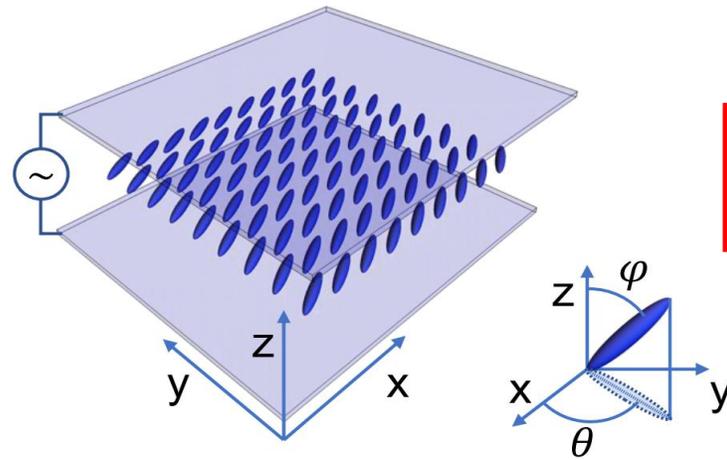
$S = 87 \pm 1\%$



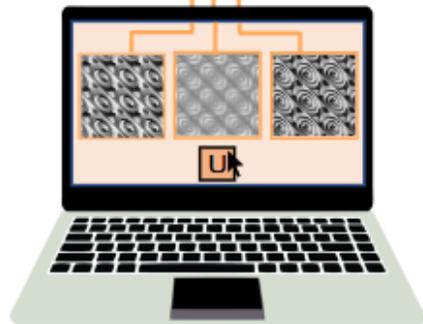
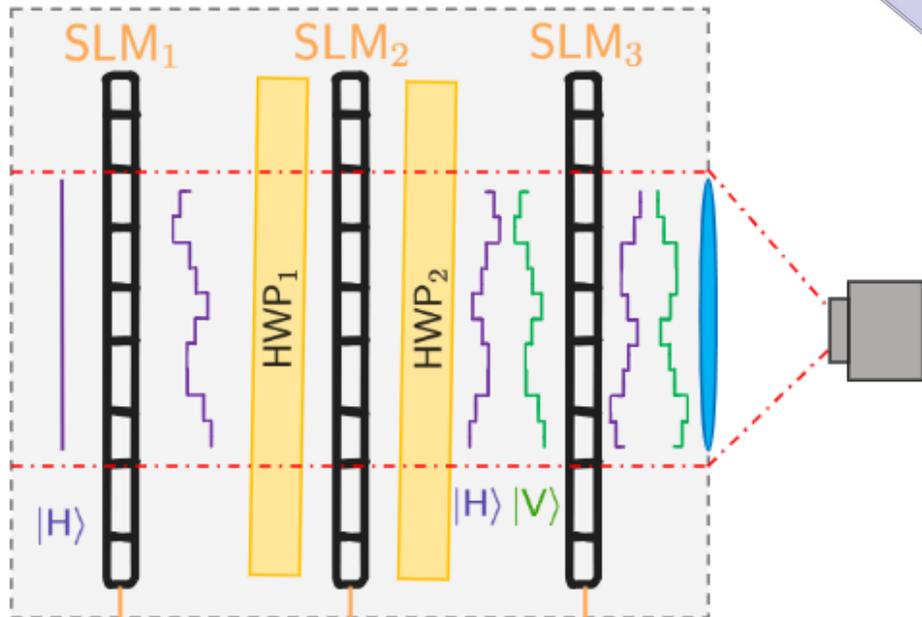
# *Programmable photonic circuit*

M.G. Ammendola et al., *in preparation*

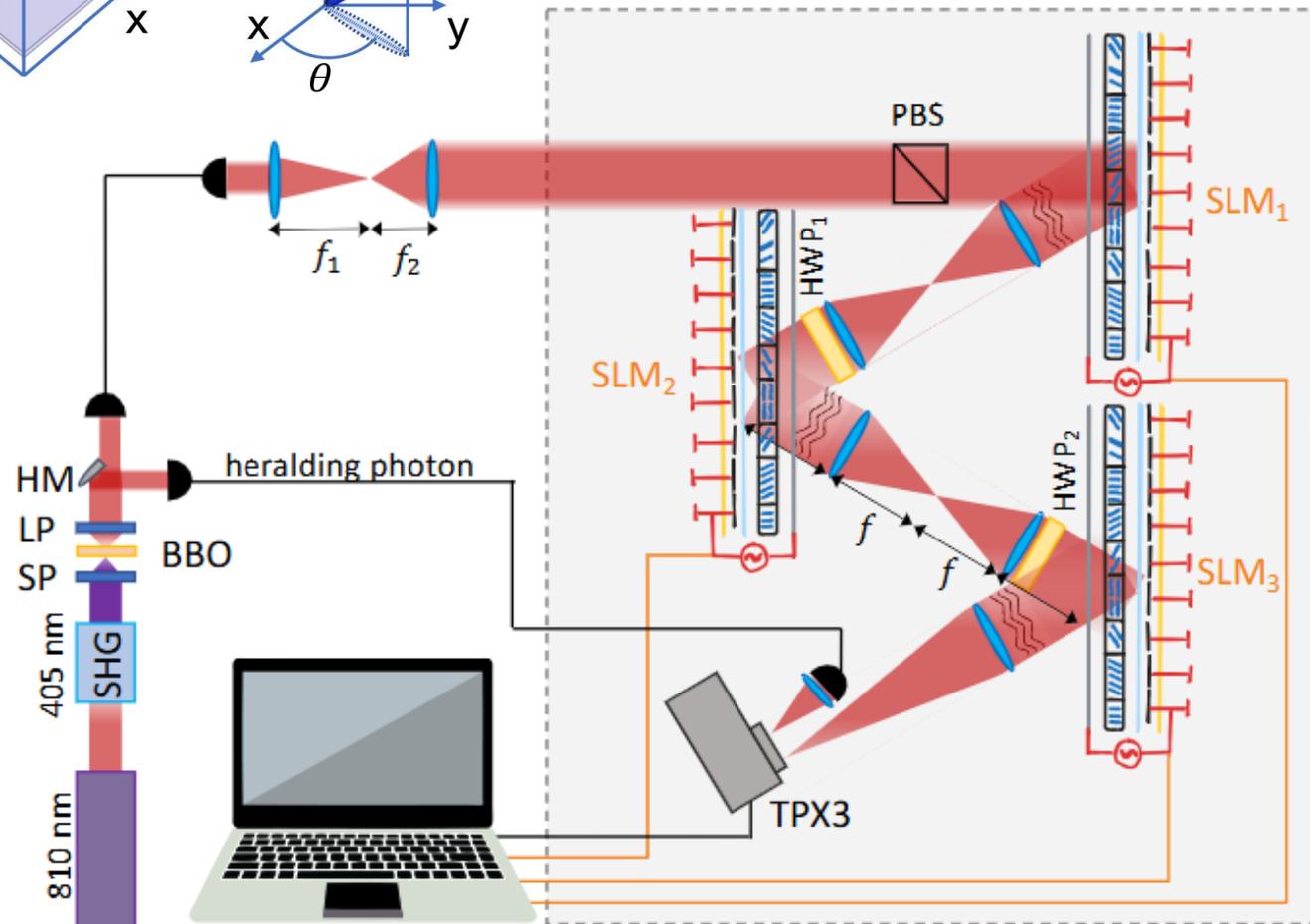
# Spatial Light Modulators



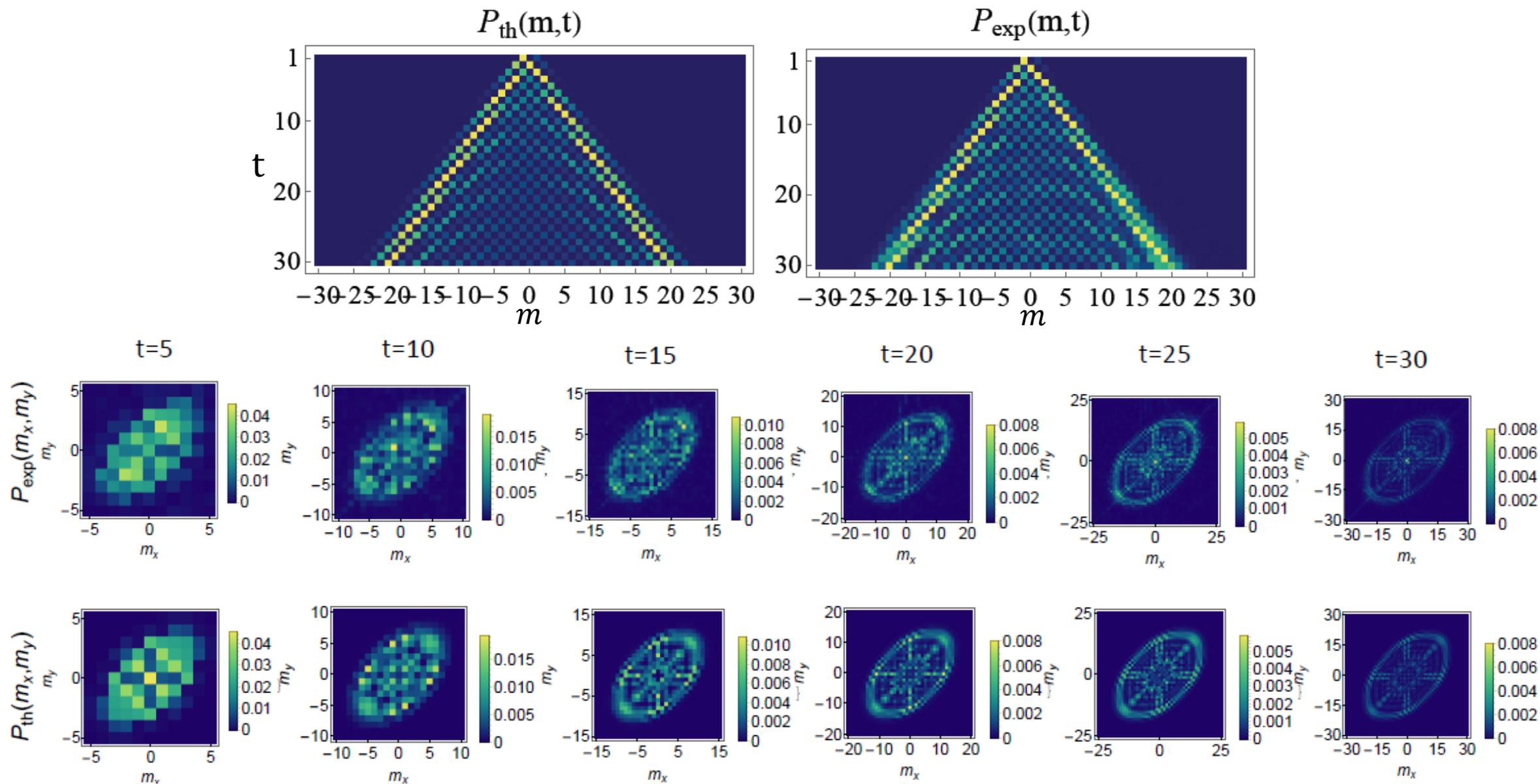
$$\theta(x, y) \rightarrow \delta(x, y)$$



Circuit control



# Results



# *Conclusions*

## Take-home message

- Compact liquid-crystal-based photonic circuits enabling extreme quantum simulations

# Acknowledgments



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# Similarity estimator

$$s = \left( \sum_m \sqrt{P_{\text{exp}}(m) P_{\text{th}}(m)} \right)^2$$

# Operator description

COIN ROTATION

$$W = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & i \\ i & 1 \end{pmatrix}$$

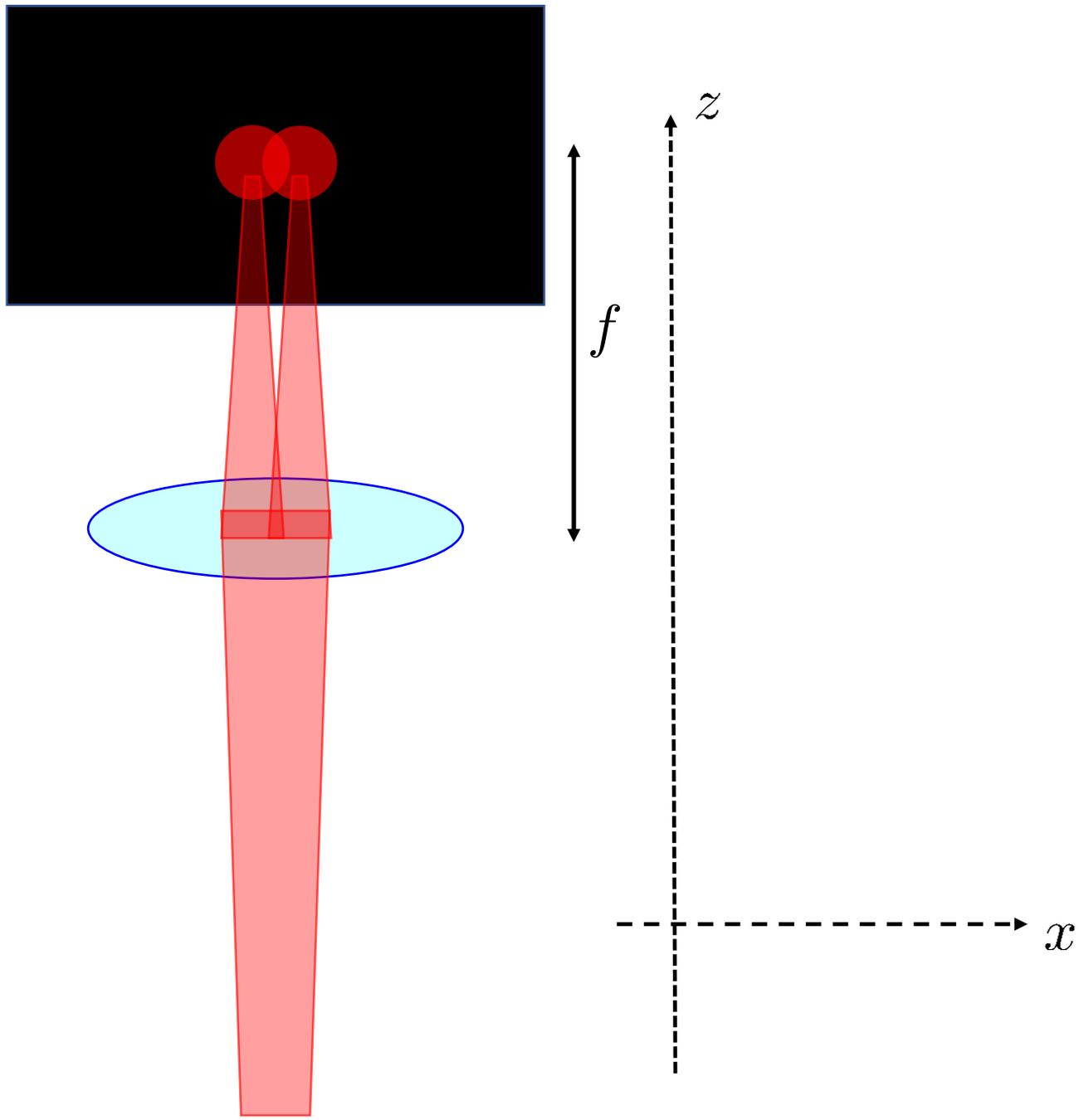
COIN-DEPENDENT TRANSLATION

$$T(\delta) = \cos\left(\frac{\delta}{2}\right) I + i \sin\left(\frac{\delta}{2}\right) \sum_m (|\uparrow\rangle\langle\downarrow| |m-1\rangle\langle m| + |\downarrow\rangle\langle\uparrow| |m+1\rangle\langle m|)$$

$$|\psi_\tau\rangle = U^\tau |\psi_0\rangle$$

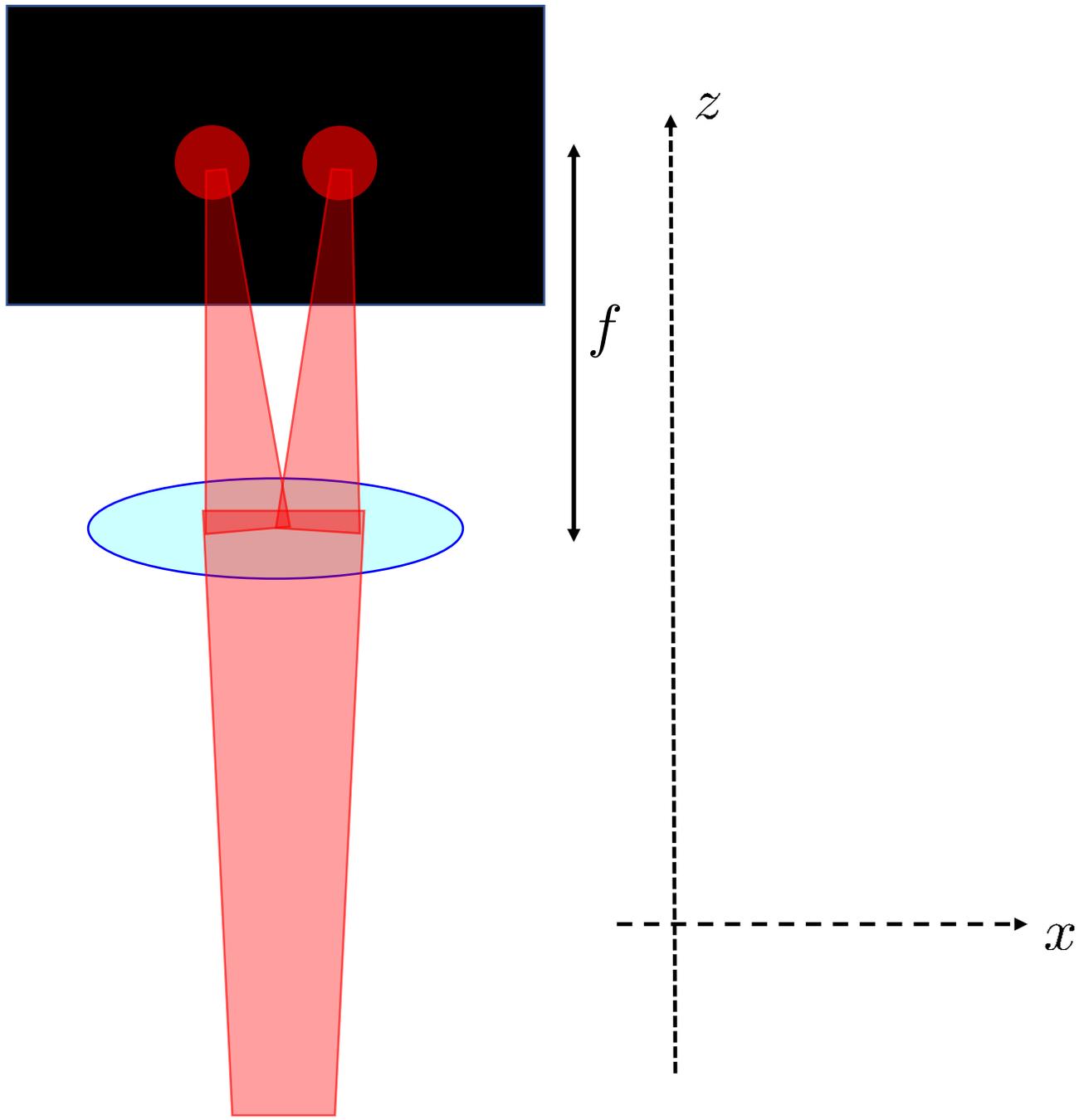
# Orthogonality?

$$\langle m|m' \rangle \neq 0$$



# Orthogonality?

$$\langle m|m' \rangle \simeq 0$$

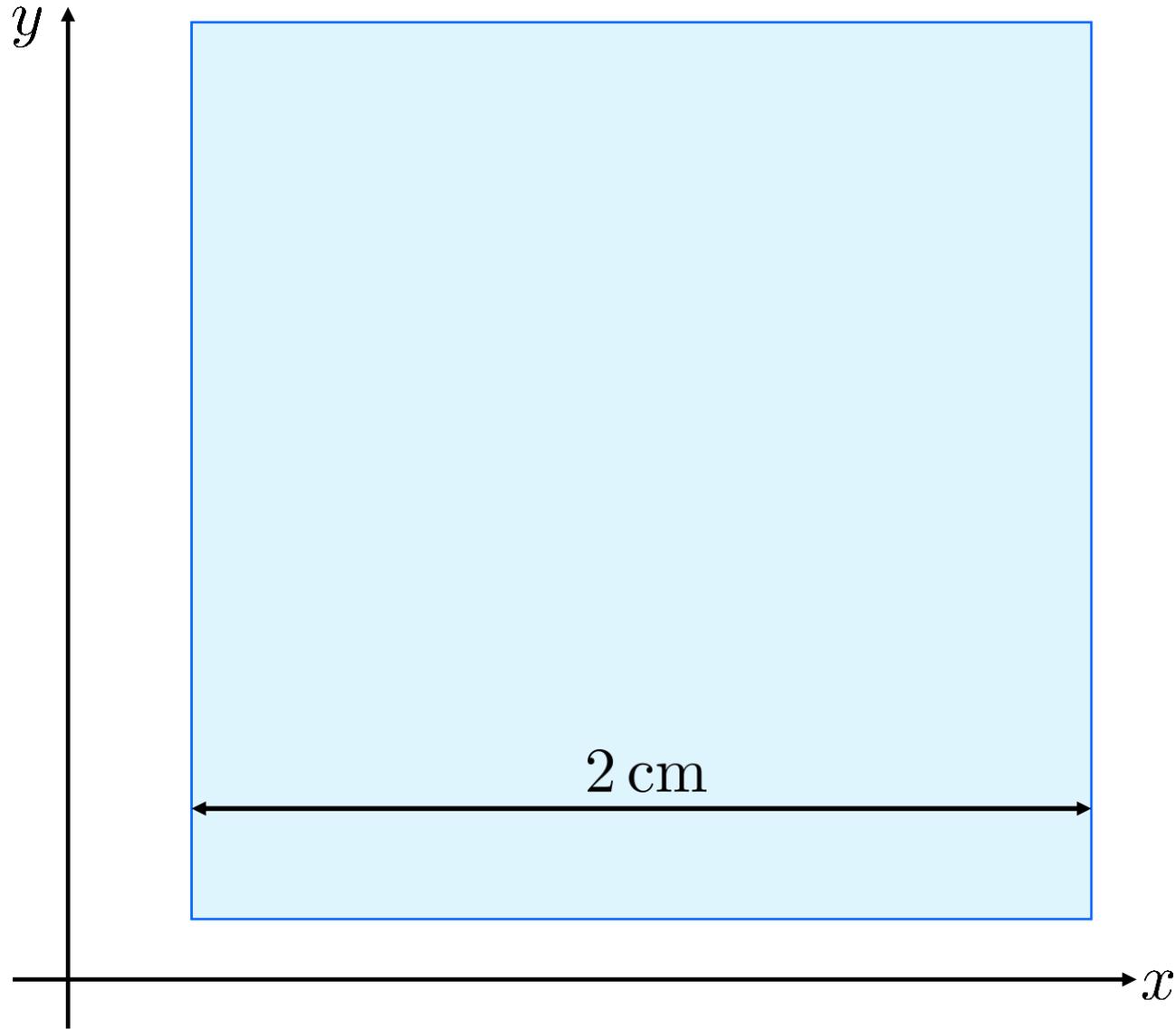


Liquid-crystal metasurfaces

LC patterned waveplates with electrically-tuned birefringence

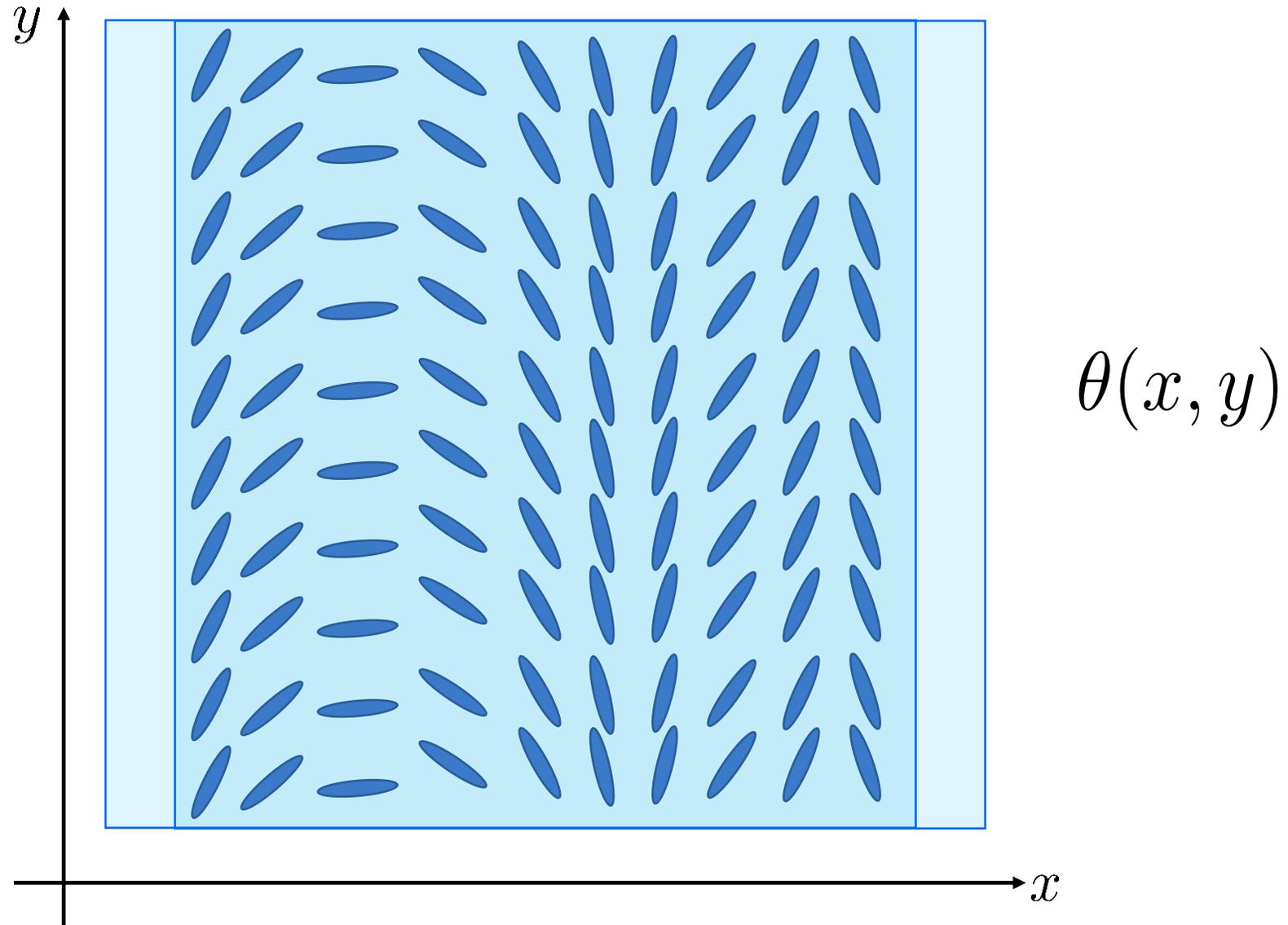
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